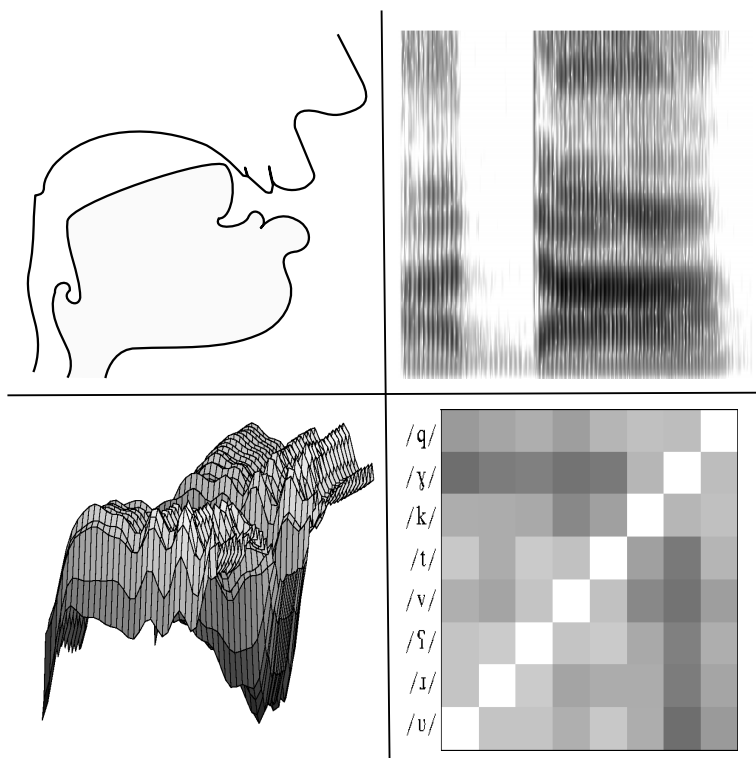


Master project Artificial Intelligence:
**Investigating consonant inventories with acoustic and
articulatory models**



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Abstract

The basic inventory of sounds (*phonemes*) used to encode speech varies considerably between languages. Nevertheless these inventories show an unmistakable preference for certain phonemes and phoneme configurations. It has often been remarked that phonemic systems seem to strike some balance between *maximal perceptual distinctiveness* and *minimal speaker effort*. Computer models formalizing these principles have yielded phonetically quite accurate results for vowel configurations. This thesis describes a computational model that attempts to apply these same principles to consonant phonemes, which are much more complex than vowels in articulatory and acoustic terms.

The model makes use of an *articulatory synthesizer* to generate speech sounds and uses *dynamic time warping* (DTW) to judge perceptual similarity between these sounds. DTW is also used to compare the resulting phonemes to those found in natural languages.

Results indicate that the model is able to arrive at a set of perceptually distinct consonant phonemes. However, the effort minimization parameter used in the model is not shown to result in more common phonemes. I argue that the model may be a useful means of researching phonological universals in consonant inventories but needs to be improved in several ways, which are discussed at the end of the paper.

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These figures were drawn in Praat (Boersma and Weenink 2009), with the following exceptions:

- Figures 1.1, 1.3, 3.1, 5.4, 5.5 and 5.6 were created in OpenOffice.org Calc.
- Figures 1.2 (adapted from Liljencrants and Lindblom 1972), 1.4 (adapted from Lindblom and Maddieson 1988), 2.1 (adapted from Boersma 1998) and 2.8 were created in the vector graphics editor Inkscape.

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Chapter 1

Introduction

1.1 Phonological patterns

Natural languages show remarkable variety in the number of different sounds (phonemes) that are used as units in speech. The conventional method of transcribing speech sounds, the International Phonetic Alphabet [IPA \(1999\)](#), uses 107 distinct symbols to encode speech sounds, and also includes more than 50 diacritics to indicate slight specifications on this basic set of symbols. Indeed, some languages distinguish between a large number of these sounds. For instance, the English phoneme inventory distinguishes approximately 45 phonemes, of which about 20 are vowels and about 25 are consonants ([Roach 2000](#)). The Khoisan language !Xóõ has the largest known phoneme inventory, with at least 58 consonants and 31 vowels ([Traill 1985](#)). Smaller phoneme inventories are more common, however; the average seems to lie somewhere between 20 and 40 ([Clark et al. 2006](#)).

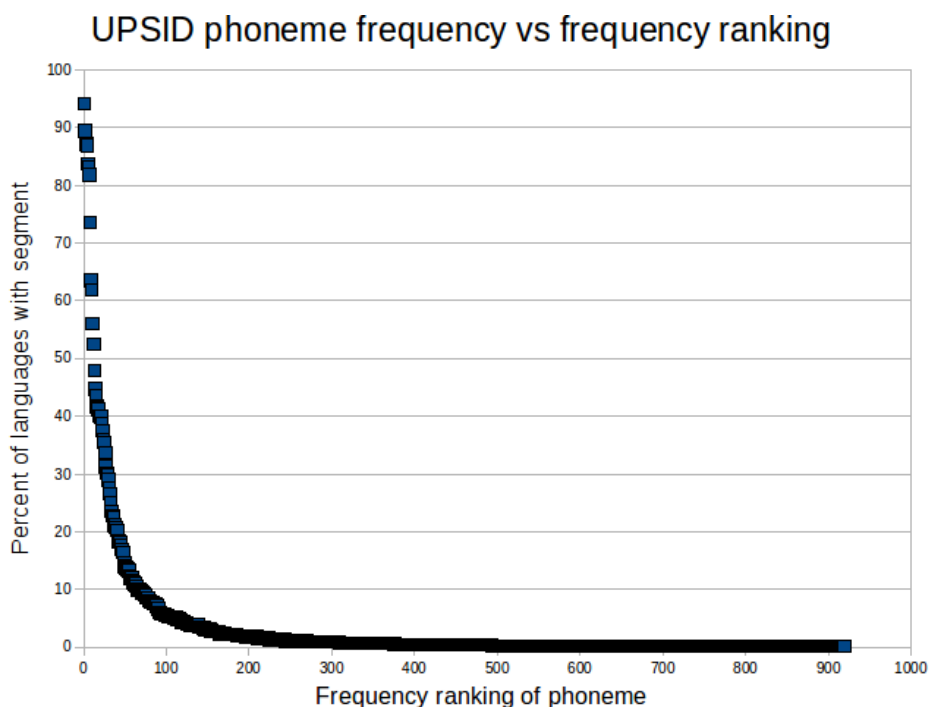


Figure 1.1: Plot of relative frequency (in percent, vertical axis) versus frequency ranking (absolute, horizontal axis) of UPSID phoneme segments

Despite this variety, the distribution of phonemes among different languages is far from arbitrary. The UPSID (UCLA Phonological Segment Inventory Database, [Maddieson and Disner 1984](#)), a statistical survey of the phonological inventories of 451 languages, shows that the consonants /m/, /k/, /p/ and /j/ and the vowels /a/, /i/ and /u/ all occur in over 80% of the languages in the database. On the other hand the front rounded vowel /y/ occurs in only about 5% of the surveyed languages, and many consonant segments are even rarer (like the click consonants of the aforementioned !Xóõ, some of which are only attested in that language). Generally the segments in the database show a Zipfian distribution ([Zipf 1949](#)), where a small number of phonemes are extremely common crosslinguistically, whereas a large number of phonemes occur only very rarely (Figure 1.1).

Looking beyond the distributions of individual phonemes, there are also common patterns to be found in the organisation of sounds within phoneme inventories. Rarer (*marked*) phonemes tend to occur more frequently in larger inventories, and the appearance of a marked phoneme in an inventory often implies the presence of a similar unmarked phoneme. For instance, the presence of the marked close rounded front vowel /y/ in a phoneme inventory implies that this language also has its unmarked counterpart, the close unrounded front vowel /i/. Tendencies of this sort are called *phonological universals*, and occur across languages that are not provably related.

Languages and their phoneme inventories are not static entities; as they are transmitted from generation to generation they are subject to change. A well-documented historical example is the branching of the Romance language family: the 10-vowel inventory of Classical Latin ([Allen 1989](#)) grew to 17 vowels in modern French and shrank to 5 vowels in modern Spanish ([Battye et al. 2000](#)). From a diachronic perspective, saying that certain phonological patterns are more common than others can be rephrased as stating that certain phonological states are more stable or attractive than others over time. However, there is considerable controversy and debate over the mechanisms behind this stability. The next section examines these different viewpoints in more detail.

1.2 Innatism versus emergentism

Broadly speaking, explanations for phonological tendencies or *universals* come in two forms. The first type of hypothesis argues that preferences for certain phonological patterns are to some extent *innate*, that is to say, hard-wired into the human capacity for language learning. The second type of hypothesis views phonological patterns as *emergent*: they arise as a consequence of phonetic properties of the phonemes themselves and the way they are transmitted. [Moreton \(2008\)](#) calls the two types of hypotheses *analytical bias* and *channel bias* respectively, and stresses that they need not be mutually exclusive.

Theories of innate phonological bias are usually connected to [Chomsky \(1965\)](#)'s theory of Generative Grammar (which primarily concerns syntax) and were made explicit for phonology in [Chomsky and Halle \(1968\)](#). Generative views on phonology often describe phonemes in terms of basic *distinctive features*. Each phoneme can be described in terms of a unique combination of these features, and sets of features can describe *classes* of phonemes which undergo some phonological process. Innatist approaches to phonological typology state that features do not merely serve a descriptive purpose: rather, the crosslinguistic predisposition toward certain feature combinations and classes suggest that there is a cognitive basis to the features.

There has also been some psychological research supporting an innate bias. For example, [Caramazza et al. \(2000\)](#) found evidence from two aphasics that consonants and vowels are processed separately, suggesting a cognitive basis for the universal phonological distinction between vowels and consonants. Indications of neurological correlates for more fine-grained

phonemic distinctions have also been found (e.g. [Eulitz and Lahiri 2004](#)).

Proponents of emergentist theories (sometimes also called *substance-based* theories) point out that many aspects of phonological typology seem to be governed by phonetic principles. One such property is *perceptual contrast*: phonological inventories tend to organize sounds in such a way that they are maximally auditorily distinct from one another. This is especially apparent in the organisation of vowel inventories. The UPSID shows that languages with three vowels overwhelmingly have the configuration (/a/, /i/, /u/) ([Maddieson and Disner 1984](#)). These three vowels are maximally dispersed in terms of their first and second formant frequencies, which are considered the most important cues in vowel perception ([Klein et al. 1970](#)). Obviously there are benefits to such dispersion: it diminishes the probability of confusing one phoneme for another, making communication in a noisy environment more efficient.

This tendency towards maximal auditory dispersion seems to be counterbalanced by a tendency toward *maximizing articulatory efficiency* (see e.g. [ten Bosch 1991](#)). According to [Boersma and Hamann \(2008\)](#), languages with only one phoneme on a given auditory continuum often place it in the center of this continuum, corresponding to an articulation which requires least effort. The Quantal Theory of [Stevens \(1972\)](#) explains phoneme distributions in both articulatory and acoustic terms: it states that languages prefer phonemes which are robust to small variations in articulations.

As the long-term acquisition of spoken language is impossible to recreate in a laboratory setting, direct empirical research into either hypothesis is not feasible. However, it can be argued that generally, emergentist explanations are more elegant: they refer to measurable properties of speech production and perception. On the other hand explanations in terms of innateness often rely on postulating complex neurological structures, about which much remains unknown and which can only be verified indirectly, at best. This means that explanations viewing phonological patterns as emergent are preferable per Occam’s Razor; if a phonological universal has a plausible explanation in emergentist terms, this eliminates the need for a more complicated model of innate bias. The next section will focus on some computational research on language and speech acquisition supporting an emergentist view.

1.3 Computer models of language and speech evolution

Over the last decades, computer modeling has gained popularity as a means of research into language evolution. These models concern both the biological evolution of language (simulating the emergence of the language faculty in our hominid ancestors) and the cultural evolution of language (simulating sound and language change). An example of the latter is the Iterated Learning Model (ILM) of [Kirby and Hurford \(2002\)](#). In this model, interaction between individuals is modeled in a simple ‘protolanguage’. Even without pressuring for efficient communication, essential properties of natural language such as compositionality and recursivity emerge spontaneously in a population of simulated learners ([Kirby 2001](#)). This indicates that linguistic structure and regularity may emerge without any *a priori* innate preference for it.

In the field of phonetics and phonology, computational research into sound systems has likewise indicated that many properties of sound systems are emergent. An pioneering study in this respect was performed by [Liljencrants and Lindblom \(1972\)](#), who found that many common vowel systems can be easily explained in terms of acoustic properties of the vowels themselves: by calculating for a given number of vowels a configuration that maximizes the distance between vowels in terms of their first and second formant, configurations closely resembling those found in many languages emerged. (Figure 1.2). These results have more recently been refined by [Schwartz et al. \(1997\)](#).

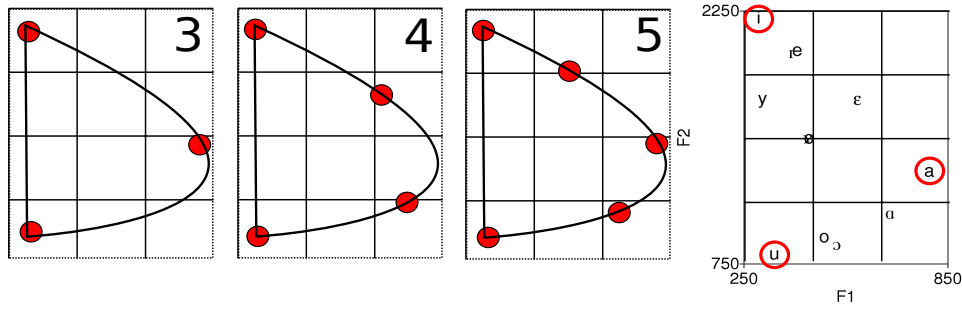


Figure 1.2: Maximizing F1/F2 distance between 3, 4 and 5-vowel configurations, adapted from Liljencrants and Lindblom (1972); the rightmost figure shows a plot of Dutch vowels for comparison (data from Pols et al. 1973), with the corner vowels /a/, /i/ and /u/ circled.

de Boer (2001) simulated the emergence of dispersed vowel systems in a population of simulated speakers (agents) without explicitly modeling a need for maximization of acoustic distance: rather, the agents strived toward minimizing communication errors, and realistic dispersion emerged in their shared language as a consequence. Oudeyer (2001) elaborated on these results with a simulation that included a simple articulation model capable of producing syllables consisting of both consonants and vowels. Zuidema and de Boer (2009) showed, again through an agent-based simulation, that phonemic coding (re-using different combinations of sounds) emerges as a better means of communication than a sound system consisting of only holistic signals. Sounds in this simulation were represented as trajectories on an abstract plane. van Leussen (2008) combined the model of de Boer (2001) with a model of phoneme dispersion by Boersma and Hamann (2008) based on Optimality Theory (Prince and Smolensky 1993) to show how articulatory effort might be incorporated in an agent-based model of vowel dispersion.

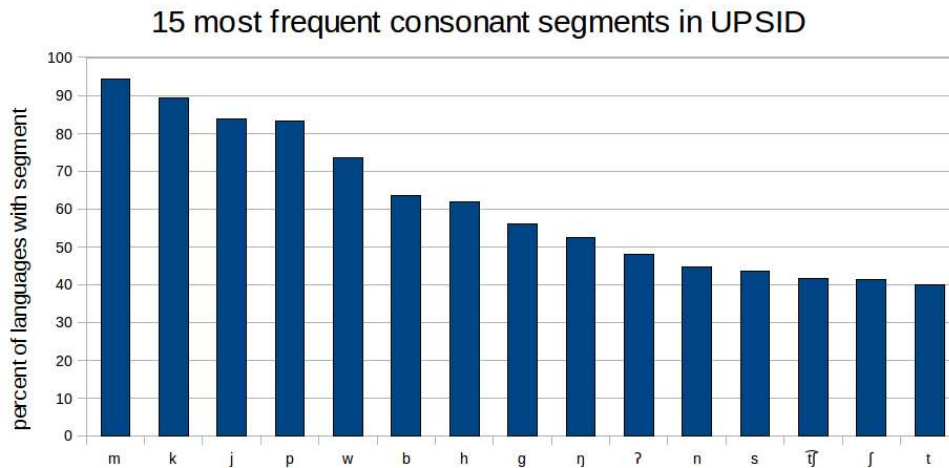


Figure 1.3: Relative frequencies of the 15 most frequent consonant phonemes in UPSID. The most frequent consonant, the bilabial nasal /m/, occurs in the inventories about 94% of the languages in the database.

1.4 Modeling consonant inventories

While computer models into phonological patterns have yielded phonetically very accurate predictions for vowel systems, modeling consonant inventories has remained more elusive. Simulations involving consonants or consonant-vowel combinations often represent the space of possible phonemes abstractly (see e.g. Boersma 1989, Mielke 2005), or in terms of their phonological features. Using predefined categories or abstractions limits the explanatory power of these simulations, since the outcome is shaped by the phonological categories assigned to the input. The reason for these abstractions must probably be sought in the difficulty of formalizing the phonetic properties of consonants.

By their nature consonants are often more complex than vowels in terms of their articulation, acoustics, and the relation between these two. Vowels can be classified quite accurately in terms of just the first and second formant frequencies (or effective second formant frequency, see Bladon 1983). Articulation of vowels is usually reduced to three dimensions: tongue height, tongue backness, and lip rounding (for example de Boer 2001). Furthermore, there is a clear monotonic correlation between these articulatory dimensions and the first and second formant frequencies (Traunmüller 1981, Ladefoged 2005). On the other hand cues for consonant perception are more numerous, harder to place on a continuum, and often depend on spectral transitions and durations rather than static qualities (Delattre et al. 1955). Articulatory aspects of consonants, particularly *manner of articulation*, often do not form a clear continuum; and there is often not a monotonic relation between articulatory gestures and acoustic properties of the resulting sound the way there is for vowels.

Nevertheless, languages show a clear preference for a small subset of consonants out of the hundreds of distinct possible consonants sounds (see Figure 1.3). Emergentist explanations of these tendencies in consonant inventories often state that the same principles that account for vowel typology apply to consonants. Figure 1.4, adapted from Lindblom and Maddieson (1988), illustrates the tension between two of these principles mentioned earlier: maximizing perceptual distinctiveness and minimizing articulatory effort. ‘Phonetic space’ is represented as an amorphous blob, indicating the difficulty of defining the acoustics of consonant phonemes on any sort of numerical scale.

This paper presents a model for finding optimal consonant configurations under the aforementioned constraints on distinctiveness and effort. If these are indeed the main forces acting upon consonant inventories, the model should predict the clear preference for certain consonants above others found in natural language (Figure 1.3). Optimizing within consonant space requires the following ingredients:

1. A means of defining the articulatory borders of the phonetic space, and generating all possible states within these borders;
2. A means of defining perceptual distance between points in this space;
3. A means of translating this perceptual distance and other properties of consonant inventories to parameters in a cost function, and a method to optimize this function.
4. A means of comparing the results of the optimization to natural language data, in order to test the the relative importance of the cost parameters in the model.

This paper will attempt to show that all ingredients are within reach using existing techniques from speech synthesis, speech recognition, and artificial intelligence. By using an *articulatory synthesizer*, articulatory properties of phonemes may be formalized, and the state space can automatically be constrained to the set of speech sounds that can be produced by human

beings - provided the synthesizer is realistic enough. Methods of defining perceptual distance between pairs of sounds have been studied extensively in automated speech recognition and related fields, and these same techniques can be used to interpret the results. Finally, finding a global optimum in a complex multidimensional landscape is at the heart of many problems in AI. While these techniques have all been applied to research into speech sound patterns in earlier studies, I believe combining them in a single model of consonant typology has not been attempted so far.

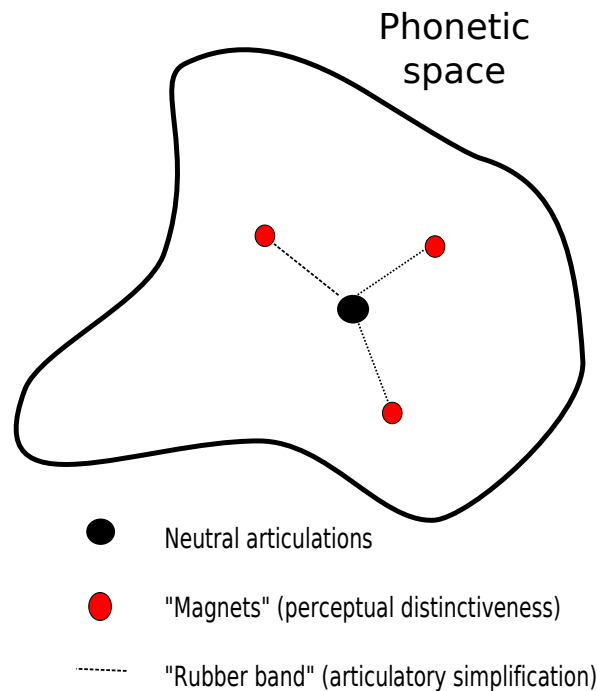


Figure 1.4: Schematic representation of the main phonetic forces acting upon consonant inventories, adapted from [Lindblom and Maddieson \(1988\)](#). Phonemes are magnetically pulled toward perceptually distinctive states, but at the same time rubber bands tie them toward neutral, less effortful articulations.

The paper is organised as follows: Chapter 2 provides more details on the different components of the model and explains some of the choices made, and Chapter 3 describes the implementation of these components in an optimization algorithm. Chapter 4 explains how the simulation outcomes may be evaluated against natural language data. Chapter 5 shows the outcome of running simulations with the model using different optimization parameters. The relevance of these results, and suggestions for future improvements on the model, are discussed in Chapter 6.

Chapter 2

Approach

2.1 Articulatory synthesis

Although mechanical emulation of the human speech apparatus has been attempted for centuries¹, nowadays the term *articulatory speech synthesis* is normally taken to mean software models. Articulatory synthesizers produce sound by modeling the movement of air through the vocal tract, which is usually represented as a series of interconnected tubes. Manipulating the width of the tubes at various points, either directly or through parameters representing the muscles controlling certain articulators in the vocal tract, affects the resulting waveforms. An early model that synthesized vowels was made by [Kelly and Lochbaum \(1962\)](#). More sophisticated models capable of synthesizing consonants and consonant-vowel combinations have also been developed (eg. [Mermelstein 1973](#), [Maeda 1982](#)); and more recently, a three-dimensional vocal tract model, based on articulatory data from MRI studies, has been developed by [Birkholz \(2005\)](#).

Articulatory synthesis is theoretically an attractive model for text-to-speech (TTS) systems, since perceived speaker attributes such as age and gender can be varied simply by changing the relevant parameters controlling the simulated vocal tract ([Shadle and Damper 2001](#)). Nevertheless, over the years commercial TTS systems have moved away from articulatory synthesis toward concatenative synthesis based on pre-recorded segments ([Klatt 1987](#), [Jurafsky and Martin 2008](#)). The acoustical calculations involved in realistic articulatory synthesis are still too demanding to perform in real-time; and despite the advances described in the previous paragraph, natural-sounding voice quality in running speech remains hard to attain.

However, articulatory synthesis has seen extensive use as a tool in phonetic and phonological research. For instance, modifications of human articulatory models have been used to investigate the vocal abilities of apes and monkeys ([de Boer 2008](#)) and Neanderthals ([Boë et al. 2002](#)). The model of [Birkholz \(2005\)](#) has been used to investigate the effect of larynx height on vowel production by [Lasarczyk \(2007\)](#).

For the research into phonetic properties of consonant inventories described in this paper, I have decided to use the articulatory synthesizer of [Boersma \(1998\)](#). The choice for this model was primarily based on the following:

- While the model is limited in its ability to synthesize vowels (Boersma, personal communication, May 2009), it is capable of synthesizing many different types of consonants, including ejectives, trills and clicks, making it well-suited for research into consonant inventories.

¹An extensive overview of the history of speech synthesis is available at the website of Haskins Laboratories: <http://www.haskins.yale.edu/featured/heads/heads.html>

- Rather than vocal tract shapes or phonologically informed gestures, the model takes muscle activity as input, which can be directly related to the notion of articulatory effort mentioned in Chapter 1.2. This also means that the model is not biased toward certain phonemes *a priori*.
- A working and scriptable version of the model is available in the software package Praat (Boersma and Weenink 2009), which conveniently can also be used for phonetic analysis of the articulations and resulting waveforms.

2.1.1 The articulatory model of Boersma (1998)

This section will provide a short overview of Boersma’s model necessary to explain its role in the simulations described in this paper, and also describes a number of limitations in its ability to synthesize consonant sounds. For an exhaustive description of the model, including the physical equations used to model airflow and movement of the vocal tract walls, the reader is referred to Boersma (1998).

A major difference between Boersma’s model and most other articulatory models is that *source* and *filter* (Fant 1970) are not independent components. Instead, the entire vocal apparatus is modelled as a series of interconnected tubes, starting at the lungs and radiating into the atmosphere at the lips and nostrils. The vocal cords are also modelled in this manner. Springs are connected to the walls of these tubes, controlling their position and stiffness (see Figure 2.1). A set of 29 muscles controls these springs; thus, the shape of the tract is ultimately determined by the activities of each of these muscles. By varying the shape of the tract over time while causing air to flow through it, speech sounds may be created.

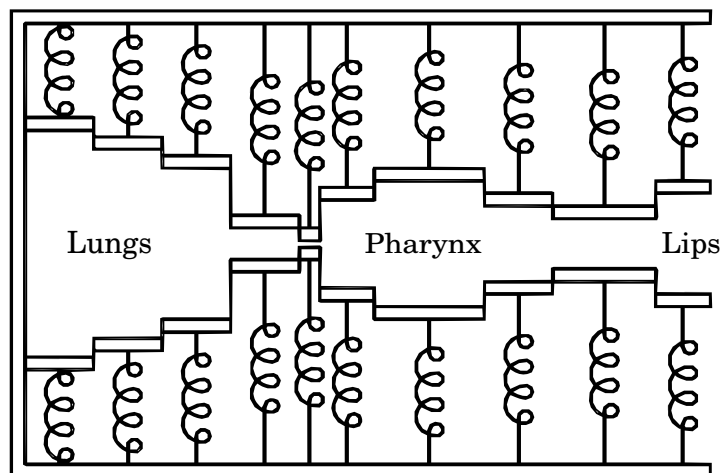


Figure 2.1: The vocal tract as represented in Boersma’s model. The position and elasticity of the walls are controlled by various muscles through springs, and by the flow of air through the tract. Neighbouring walls are also connected by springs. Acoustic output is determined by the airflow radiating into the atmosphere at the lips (and at the nostrils; the nasal tract is not shown in this figure). Adapted from Boersma (1998).

Utterances in the model are specified as a series of muscle activity targets on a timeline running from zero to a user-specified length. These targets represent muscle activity as a variable between zero (at rest) and one (fully contracted)². By default two targets are specified

²The activity parameters may actually also take on negative values. However, since these are not necessary to produce realistic articulatory movements and represent an anatomical impossibility (muscles may only contract in one direction), the activity parameters are kept within the range of [0,1] in the model described herein.

for each muscle: zero activity at the start of the utterance, and zero activity at the end of the utterance. The amount of activity at a given point on the timeline is linearly interpolated between target points. By setting a nonzero target for a muscle on a point on the timeline, contraction of this muscle is initiated, resulting in movement of the associated articulator.

As an example, creating a 0.5 second utterance that sounds like /əβə/ requires setting at least four muscle parameters:

- To cause an outward movement of air, the air in the lungs must be compressed. This is done by decreasing the *Lungs* parameter from 0.1 at 0 seconds to 0.0 at 30 ms.
- To make the vocal cords vibrate when air passes them, they must be tensed somewhat, but not completely (which would close them and prevent air from escaping). This is done by setting the *Interarytenoid* parameter to 0.5 throughout the utterance.
- To make sure air only escapes through the mouth, the velum must be raised so that the nasal tract is closed off. This is done by setting the *LevatorPalatini* parameter to 1 throughout the utterance.
- To create a transition from the vowel /ə/ to the consonant /β/ and back again, the lips must be brought close together (but not closed) in the middle of the utterance. This is done by setting the *OrbicularisOris* parameter to 0.7 between 200 and 300 ms. To make sure the vowel quality remains constant for an instant before and after articulation of the consonant, this same parameter is kept at 0 between 0 and 100 ms and between 400 and 500 ms.

Figure 2.2 illustrates the effect of superimposing these muscle gestures on a male-like vocal tract.

A variety of different consonant sounds can be synthesized in this manner; nevertheless, there are also sounds that cannot be synthesized convincingly with the articulatory model as set out in Boersma (1998). Most notably, I have not been able to synthesize natural sounding nasal consonants (/m/, /ŋ/, /n/, /ɲ/, /ɳ/ and /ɷ/). Articulatory, nasal consonants are characterized by a complete closure somewhere in the oral cavity, so that all air flows out through the nose. Acoustically this results in a sound with clearly distinguishable formants, which are however much fainter than in vowels (Ladefoged 2005). While Boersma’s model does allow for the modeling of these types of consonants by creating an oral closure and lowering the velum, the resulting sound cannot be said to resemble a nasal consonant (Figure 2.3).

The class of sibilant fricatives (/s/, /z/, /ʃ/, /ʒ/, /s/ and /z/) also cannot be synthesized well. This class of sounds is characterized by a high amount of noise in the upper region of the auditory spectrum, which is caused by a jet of air directed against the upper teeth through a narrow constriction between the tongue and the roof of the mouth. The aerodynamic calculations required for modeling this process are not incorporated in the articulatory model (Boersma, personal communication, June 2009).

These limitations, which are intrinsic to the model, regrettably constrain the number of speech sounds that can be explored using Boersma’s model. Some of these limitations only became apparent after significant time had already been invested in incorporating this articulatory synthesizer into the model. The following section will explain some additional constraints which I imposed to prevent the search space from growing too large.

2.1.2 Constraining Boersma’s model to explore consonant space

Because input to Boersma’s model comes in the form of parameters specifying muscle activity, it is very well suited to computational exploration of the phonetic space available to humans

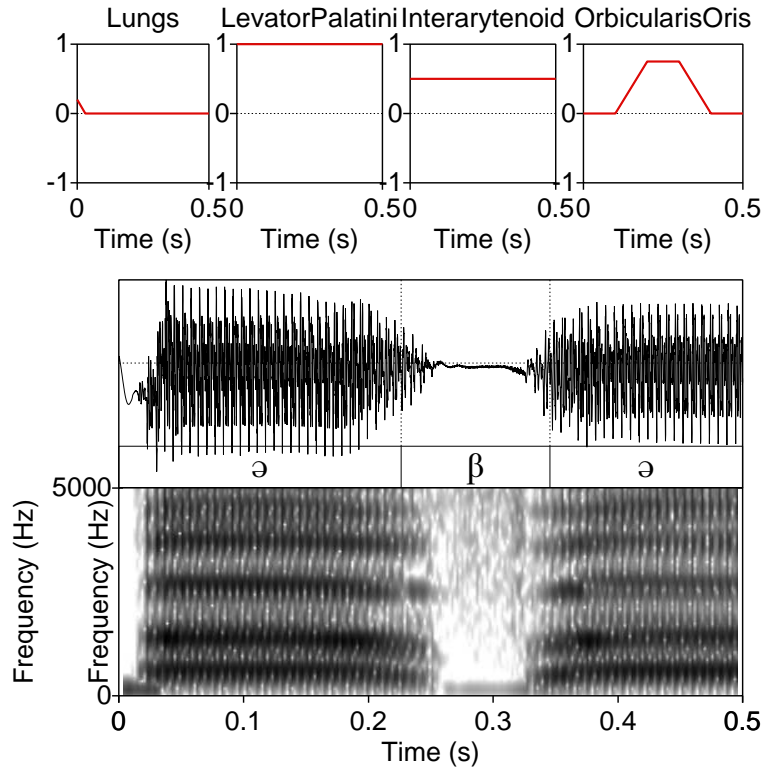


Figure 2.2: Synthesizing an /əβə/-like utterance in a male voice. The top graphs show the values of the muscle parameters over time; the middle figure shows an annotated oscillogram of the sound; the bottom figure is a spectrogram of the sound.

in the production of consonant sounds. However, the realism of the model comes at a high computational cost: at the moment of writing, synthesis of a single 0.5 second utterance takes several seconds on a reasonably modern personal computer. Any search of articulatory space will therefore be severely bottlenecked by the synthesis component. Furthermore, since only a small number of muscle movements will actually cause the airflow necessary to produce speech, a lot of search time may be wasted on finding articulations that result in any sound at all, rather than those that produce distinct consonants. To keep the time taken by the simulations within acceptable bounds, it was necessary to put some constraints on the articulations that are tried during search, both in terms of the muscle parameters used and in terms of their temporal specification.

An important constraint is that of the 29 muscle parameters available in the model, I allow only a subset of 14 to change during search. Specifically, only muscle parameters that control the tongue, mouth and oropharyngeal cavity can be changed. I will call this subset of muscles \mathcal{M} . Table 2.1 and Figure 2.4 give an overview of the muscles used and their effect on vocal tract shape. The other muscles are not used in the articulations produced during search, with the exception of the following parameters which are standard for each articulation:

- The *Lungs* parameter is set to 0.1 at 0 ms and to 0.0 at 30 ms to create air pressure in the vocal tract.
- The *InterArytenoid* parameter is set to 0.5 throughout the utterance to create phonation when air passes the vocal folds.
- The *LevatorPalatini* parameter is set to 1.0 throughout the utterance, sealing off the nasal

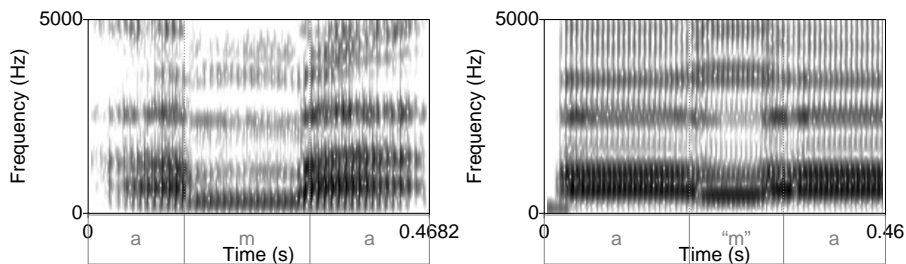


Figure 2.3: A spectrogram of a real male speaker saying /ama/ (left) and of a synthesized male speaker making /ama/-like articulatory movements in Boersma’s model (right). The fainter formants associated with nasal consonants are not reproduced faithfully in articulatory synthesis; the resulting utterance sounds more like /ala/.

tract.

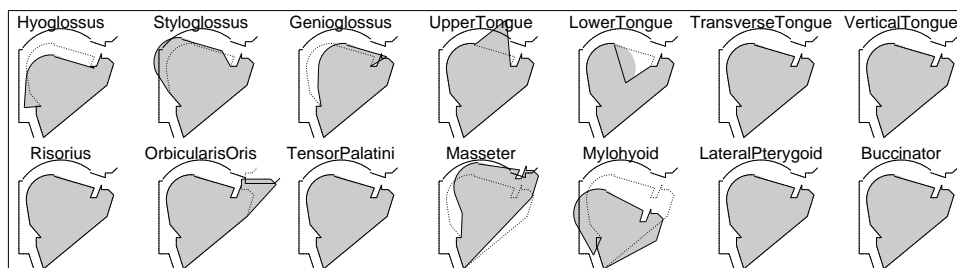


Figure 2.4: Overview of muscle parameters that are changed during search, showing a sagittal cross-section of the vocal tract when the value of that parameter is 1. Note that some muscles do not show a change in tract shape, as they either control tenseness rather than position of a wall, or cause only lateral movement.

A second important constraint is that I limit the time during which the activity of the muscles can vary. The consonant segments tried during search are embedded in an unchangeable /ə_ə/ environment: that is, they are preceded and succeeded by the neutral vowel *schwa*, which is produced by making the vocal cords vibrate while keeping the nasal tract closed and relaxing the tongue and mouth muscles. The choice of *schwa* should prevent the vowel context from exerting too large an influence on the consonants. To make sure the beginning and end of the produced utterances remain constant, the muscle parameters are fixed at zero during the vowel segments, and may only take on another value in the middle segment. During this middle segment their value also remains fixed: movement of articulators only takes place during a transitory period between the vowel and consonant segment (Figure 2.5). With these constraints, we can define the activity of a muscle m from the set \mathcal{M} using a single real-valued parameter a_m , and define a consonant segment c as a set of activity values $\{a_{m_1}, a_{m_2} \cdots a_{m_n}\}$, where $n = |\mathcal{M}|$.

2.2 Creating a cost function for consonants

The articulatory model of Boersma, described in the previous section, is able to generate a state space for our model of consonant distribution. To optimize in this space, it is necessary to find a cost function that reflects proposed optimal properties of consonants and consonant inventories. Two of these properties will be investigated in this paper: *maximal perceptual*

Table 2.1: List of muscle parameters in the articulatory model of Boersma (1998). Note that some of these muscles have overlapping functions, while others are antagonists of one another, i.e. pull the articulators into opposite directions. Only a subset of these 29 muscles is explored in the optimization model described in this paper. The rows shaded gray represent parameters for which the value is fixed during search; the unshaded rows are the subset of muscles \mathcal{M} that are explored in search.

Name of muscle (group)	Function
<i>Buccinator</i>	Tenses oral walls
<i>LateralPterygoid</i>	Moves jaw horizontally
<i>Mylohyoid</i>	Lowers mandible, opening mouth
<i>Masseter</i>	Raises mandible, closing mouth
<i>TensorPalatini</i>	Lowers velum
<i>OrbicularisOris</i>	Purses lips
<i>Risorius</i>	Spreads lips
<i>VerticalTongue</i>	Makes tongue thinner
<i>TransverseTongue</i>	Makes tongue thicker
<i>LowerTongue</i>	Lowers tongue tip
<i>UpperTongue</i>	Raises tongue tip
<i>Genioglossus</i>	Moves tongue forward
<i>Styloglossus</i>	Moves tongue back and upwards
<i>Hyoglossus</i>	Moves tongue downwards
<i>LevatorPalatini</i>	Raises velum
<i>Sphincter</i>	Constricts pharynx
<i>UpperConstrictor</i>	Constricts upper part of pharynx
<i>MiddleConstrictor</i>	Constricts middle part of pharynx
<i>LowerConstrictor</i>	Constricts lower part of pharynx
<i>Thyropharyngeus</i>	Constricts ventricular folds
<i>Sternohyoid</i>	Lowers larynx
<i>Stylohyoid</i>	Raises larynx
<i>LateralCricoarytenoid</i>	Opens glottis
<i>PosteriorCricoarytenoid</i>	Closes glottis
<i>Thyroarytenoid</i>	Relaxes vocal folds
<i>Vocalis</i>	Tenses vocal folds
<i>Cricothyroid</i>	Tenses vocal folds
<i>Interarytenoid</i>	Adducts vocal folds
<i>Lungs</i>	Expands lungs

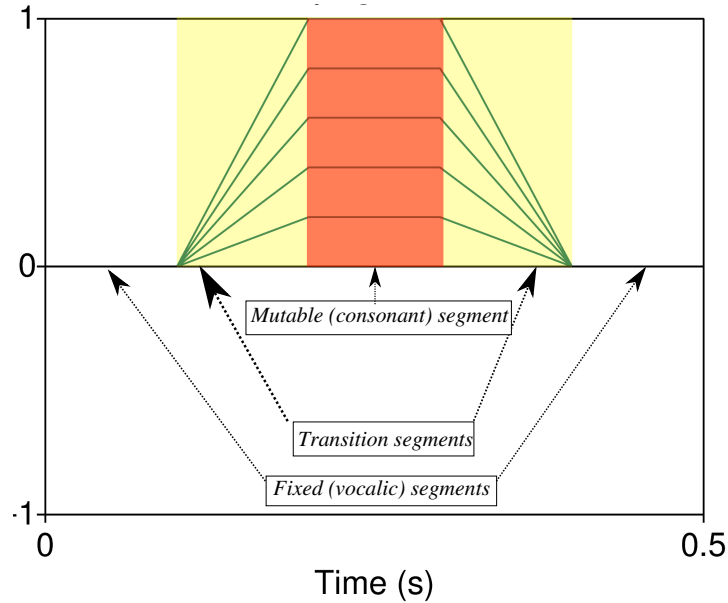


Figure 2.5: A graph representing possible articulatory movement over time for the 14 muscles that are used in search. A single real-valued parameter between 0 and 1 represents the activity of a given muscle during the middle (consonantal) segment. The activity will be 0 (relaxed) during the vowel segment, and movement from zero activity to the specified level of activity takes place in the transition segment.

contrast and *minimal articulatory effort*. The first is a property of consonant *sets* which can be derived by comparing the waveforms of different utterances generated by the articulatory synthesizer; the second is a property of consonants *themselves*, and can be derived directly from the muscle activity patterns which serve as input to the synthesizer.

2.2.1 Defining perceptual distinctiveness

Computational models of vowel systems usually define perceptual distance using some weighted combination of their first and second (and sometimes third and fourth) formant values, which numerous perception experiments have shown to be the primary cues for vowel perception. Cues for consonant perception are also to be found in the spectrum. For example, in languages that have a contrast between voiced and voiceless plosives, an important cue that determines whether voicing is perceived is Voice Onset Time (VOT), the time elapsed between release of a plosive and the start of vocal cord vibration (Lisker and Abramson 1963). However this same cue plays no role in the perception of sibilant fricatives, which are primarily identified through the location of intensity peaks in the spectrum (Harris 1958). Cues for place of articulation are often found in formant transitions, making them dependent on the preceding and following segments. Clearly, combining these different types of cues into a single perceptual distance metric is not as straightforward as it is for vowels.

The problem of defining a global measure of perceptual contrast is briefly considered by Boersma (1998). However, he ultimately dismisses the notion of a global contrast measure as “linguistically irrelevant”, since perceptual difference is known to depend heavily on the language(s) the hearer is proficient in; the language one is exposed to can determine the perceived contrast between two segments (e.g. Kazanina et al. 2006). This holds true when modeling language at the level of the speaker, but as the model described in this paper concerns crosslinguistic notions of optimal distance, a global distance metric is indeed relevant. Furthermore, the ubiquity of certain types of vowel systems mentioned in Maddieson and Disner (1984), and

research on perception of speech sounds by nonhuman animals (e.g. [Kuhl 1981](#)) indicate that perceptual distance is at least partially grounded in common properties of mammalian hearing.

At this point it is instructive to take a look at best practices in the area of automatic speech recognition. After all, speech recognition is also concerned with mapping an incoming speech signal to a best fit among a set of stored signals. An effective metric of similarity between segments is therefore desirable for accurate recognition. The next section describes how one such measure, dynamic time warping on mel-frequency cepstral coefficients, can be used as an effective method for computing perceptual distance between two consonant segments.

2.2.2 Measuring perceptual distance with DTW and MFCCs

Dynamic time warping (DTW) is an algorithm for measuring similarity between two signals or sequences, which is robust to variations in time and speed (speaking rate). Both signals are divided into a number of frames, which contain vectors representing features or measurements from that point in the signal. A matrix representing the distance between each frame of the first signal and each frame of the second signal may be computed according to some distance function defined on the feature vectors. The least costly path through this matrix may then be computed, for instance using the Viterbi algorithm ([Viterbi 1967](#)). The length of this path represents the ‘warp’ or distance between the two signals. The accuracy of DTW as a distance measure can be improved by placing some constraints on the minimum and maximum slope of the path ([Sakoe and Chiba 1978](#)).

Perceptual features for comparing speech signals can be extracted by dividing the power spectrum into a number of frequency bins and taking the power of the signal inside each of these bins. Because human hearing is not organized along a linear scale, more accurate feature vectors can be created by first transforming the sound signals to the psychoacoustic Mel scale ([Stevens and Volkman 1940](#)) using mel-frequency cepstral coefficients (MFCCs, [Bridle and Brown 1974](#); [Davis and Mermelstein 1980](#)). MFCCs are a fairly effective metric for the recognition of isolated segments (e.g. [Sroka and Braida 2005](#)) and are also used in the field of automatic music recognition and retrieval ([Tzanetakis and Cook 2002](#)). Employing DTW as a measure of perceptual distance between phonemes was inspired by [Mielke \(2005\)](#).

For this paper, I have used the MFCC and DTW implementations of Praat ([Boersma and Weenink 2009](#)), using the standard settings for creating MFCCs from waveforms. Under these settings, the sound is divided into windowed frames of 15 ms, with a sampling period of 5 ms, and 12 mel-frequency cepstral coefficients are calculated on these frames using the method described in [Davis and Mermelstein \(1980\)](#). Distances between frames can then be calculated as a weighted sum of three components:

1. euclidean distances between the cepstral coefficients
2. euclidean distance between the log energy (loudness) of frames
3. the regression coefficient of the cepstral coefficients over a number of subsequent frames

However, weights (2) and (3) were set to zero in the experiments described in this paper, as they did not seem to have a positive effect on the effectiveness of the distance metric. Therefore the mutual distance d_{ij} between two MFCC frames i and j is calculated with the formula

$$\sum_{k=1}^{numCoefficients} (c_{ik} - c_{jk})^2 \tag{2.1}$$

where $numCoefficients = 12$ and c_{ij} is the j th coefficient of frame i . The optimal Viterbi path through the matrix of frame distances is then calculated, with the constraint that the first

and final frames of the two signals match, and that the path lie between two lines with slopes $\frac{1}{3}$ and 3.

Figure 2.6 shows DTW paths for comparisons of a male speaker saying /asa/, /apa/ and /aza/. In terms of phonological features, the segment pair /s/-/p/ is more distant than the pair /s/-/z/; the first pair differs both in place of articulation (ALVEOLAR vs BILABIAL) and manner of articulation (FRICATIVE vs PLOSIVE), the second pair only in voicing (VOICELESS vs VOICED). This is reflected by a shorter DTW path for the pair /asa/-aza/.

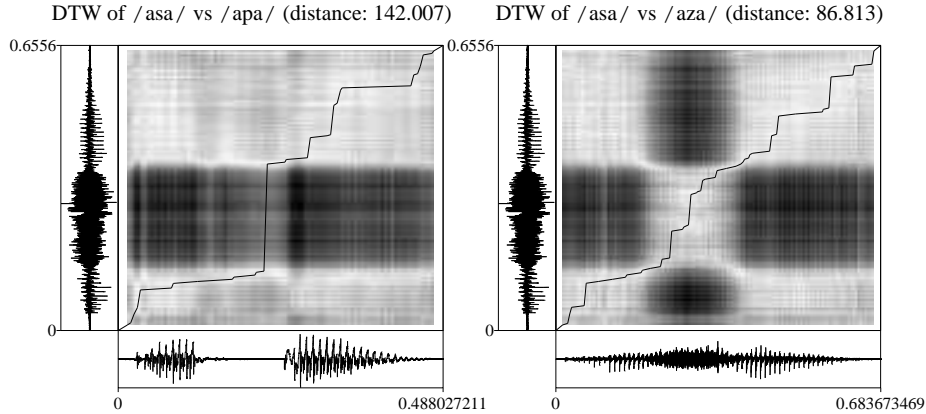


Figure 2.6: An illustration of dynamic time warping on two pairs of MFCCs. Left shows /asa/ (vertical) versus /apa/ (horizontal), right shows /asa/ (vertical) versus /aza/ (horizontal). The distance matrices are shown, with darker cells representing a greater distance. The more the path through the matrix resembles a straight line, the smaller the distance between the two signals.

The length of the paths calculated between MFCC representations of two sounds thus provides a metric that may correspond to the perceptual distance between these two sounds. Figure 2.7 illustrates that the DTW distance corresponds quite well with phonologically informed ideas of perceptual distance, clustering a number of natural classes together.

As said, the distinctiveness of a consonant segment s is not an intrinsic property of consonants themselves, but must be stated in terms of its relation with the other segments in the inventory \mathcal{S} . Let us define the mutual perceptual distance between two sound signals created from a pair of consonant segments s_1 and s_2 as $DTW(s_1, s_2)$. We then define a cost function over the perceptual distinctiveness d of a given segment s as the *smallest distance* between it and the other sounds in the inventory \mathcal{S} :

$$d(s) = \frac{50}{\min_{s_j} (DTW(s, s_j))} \text{ such that } s \neq s_j \quad (2.2)$$

This metric will be used as a variable that is to be minimized during search; hence the choice to used *inverted* distance for distinctiveness cost. The choice of 50 as a numerator was to ensure that the values for $d(s)$ lie in approximately the same range as the effort values discusses in the next section. DTW will also be used as a method to interpret the results of the simulations (4.2).

2.2.3 Defining articulatory effort

The observation that speakers aim to reduce the amount of effort they spend on enunciating has often been made, both in connection to running speech and to the organization of sounds

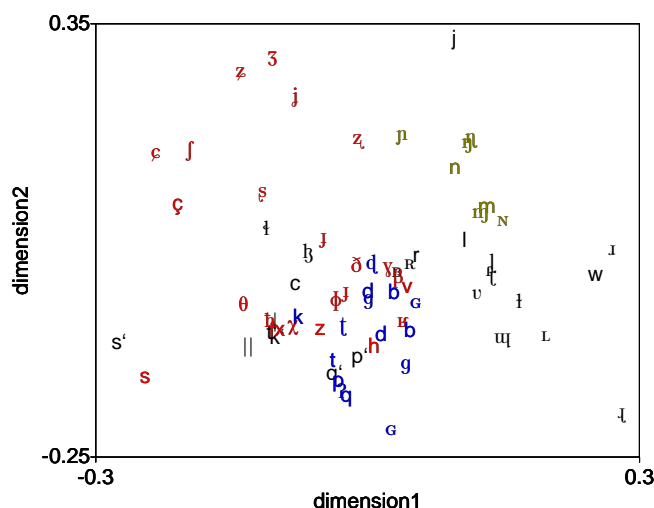


Figure 2.7: A scatterplot representing the DTW distances between 60 phonemes in an /a_a/ context. For visualization purposes, the 59-dimensional space has been reduced to two dimensions using individual difference scaling (as implemented in Praat’s INDSICAL function on distance matrices). Nasal sounds are drawn in green, fricatives in red, and plosives in blue; other categories (trills, taps, clicks, ejectives, affricates, laterals and approximants) are drawn in black

in inventories; but formalizing the notion of ‘articulatory effort’ is difficult (e.g. [Trubetzkoy 1939](#)). Nevertheless, since the articulatory model used for this research receives input in the form of parameters which directly or indirectly represent muscle contraction, we can employ these parameters in a (naive) approximation of articulatory effort.

A first approximation of an effort function $e(s)$ over segments would be to simply sum the activities of the muscle parameters during the mutable middle segment, as in [2.3](#). This favors articulations which are articulatorily close to a neutral articulation, as well as articulations which utilize a smaller number of muscles.

$$e(s) = \sum_{m \in \mathcal{M}} a_m \quad (2.3)$$

This would divide articulatory cost equally among the different muscles. However, the amount of tissue that is moved by contracting each of the muscles in this set varies considerably. Giving activation of the *UpperTongue* parameter, which only raises the tongue tip, the same weight as the *Masseter* parameter, which raises the entire lower jaw, is probably too crude an assumption. We can approximate articulatory cost more closely by taking into account the amount of mass displaced by activation of each of the muscle parameters.

Praat allows the calculation of a *VocalTract* vector from an articulation, which contains the cross-sectional areas (in m^2) of all tubes in the modeled vocal tract at a particular time. The approximation displacement_m of the amount of area moved by a muscle m can be given by comparing two *VocalTract* vectors: one representing the shape of the tract when this muscle is fully contracted, and one representing the shape of the neutral articulation s_{neut} , i.e. when all muscle parameters are set to 0 (creating the sound /ə:/). The summed absolute difference between each of the tubes in the *VocalTract* objects of s_{neut} and s_m was then taken as the value for displacement_m . [Table 2.2](#) shows the values for all 14 muscles in \mathcal{M} . We can now define a slightly more informed version of equation [2.3](#):

Table 2.2: Values representing the displacement of vocal tract walls caused by setting each of the muscle parameters to 1 (compared to a neutral vocal tract). These values are used to give more articulatory effort ‘weight’ to some muscles.

Name of muscle (group)	Displacement
<i>Hyoglossus</i>	0.014
<i>Styloglossus</i>	0.012
<i>Genioglossus</i>	0.012
<i>UpperTongue</i>	0.009
<i>LowerTongue</i>	0.002
<i>TransverseTongue</i>	0
<i>VerticalTongue</i>	0
<i>Risorius</i>	0
<i>OrbicularisOris</i>	0.004
<i>TensorPalatini</i>	0
<i>Masseter</i>	0.021
<i>Mylohyoid</i>	0.032
<i>LateralPterygoid</i>	0
<i>Buccinator</i>	0

$$e(s) = \sum_{m \in \mathcal{M}} a_m \cdot (1 + displacement_m)^2 \quad (2.4)$$

This definition of effort has the desirable property that articulations involving large movements are punished more severely in the optimization search, and should suffice for this exploratory study. However it is admittedly somewhat arbitrary and ignores many factors that probably also play a role in effort. Chapter 6 discusses a number of ways the effort function might be made more realistic.

2.2.4 Combining effort and distinctiveness into a cost function

Having established definitions of effort $e(s)$ (Equation 2.4) and distinctiveness $d(s)$ (Equation 2.2) over a consonant segment s , they can be combined into a single cost function $f(s)$

$$f(s) = (w_d \cdot d(s) + w_e \cdot e(s)) \quad (2.5)$$

where w_d and w_e are real-valued weights between 0 and 1 such that $w_d = (1 - w_e)$. Figure 2.8 summarizes how the different components of articulation and perception combine in the cost function. With this function we can test the optimization model as a means of formalizing optimal properties of consonant inventories. In Chapter 5, this is done by varying two parameters: the size of the segment inventory \mathcal{S} and the relative importance of effort weight w_e versus distinctivity weight w_d in the cost function.

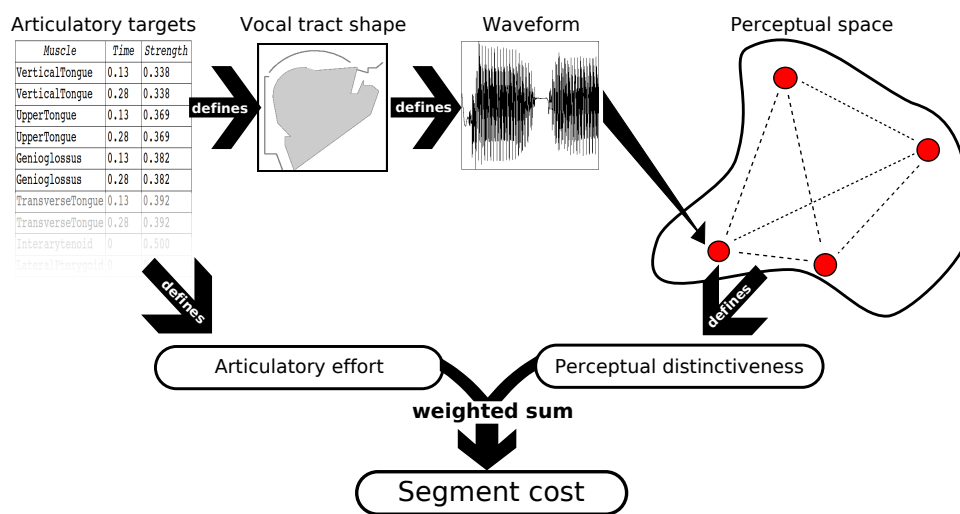


Figure 2.8: Summary of how a cost function is derived from a set of articulatory targets. The articulatory cost is directly defined by the amount of muscle activity set in the list of targets. The perceptual cost is defined by the smallest DTW distance between the synthesized segment and the other segments in the inventory. Total cost is a weighted combination of these two components.

Chapter 3

Search method

This chapter explains the search method used to find consonant inventories using the constraints and costs set out in Chapter 2. A variation of hill-climbing is used to find a set of segments that is optimal under these constraints. Section 3.2 gives an overview of the algorithm in pseudocode. A complete collection of Java and Praat code used for the experiments can be found at the author’s website¹.

3.1 Searching a complex landscape

Chapter 1.4 briefly discussed the complex nature of perceptual distance, articulatory effort and the relation between these two in consonant inventories. Figure 3.1 illustrates the consequences of this complexity for the optimization model described in this paper. It shows a transition from the neutral segment *s_{neut}* to a segment where the parameter *UpperTongue* (which raises the tongue tip) is fully active, in 20 increments of 0.05. The curves show the DTW distance from this segment to a neutral segment /ə:/, to a segment containing a bilabial plosive /əpə/, and to the previous value of the *UpperTongue* parameter. While increasing muscle activity (and thereby effort) generally increases the perceptual distance to the neutral articulation, the relationship between activity of the *UpperTongue* parameter and perceptual distance to the segment /əpə/ does not show any linearity. The amount of change wrought by an increment of 0.05 also fluctuates considerably.

It can be assumed that the actual state space for our optimization problem, which involves mutual distance between multiple segments and multiple active muscles per segment, is many times more complex. As a result the state space will contain a large number of local minima. Because of this, it is necessary to ensure that the distance between neighbouring states is initially large, to avoid getting stuck in local minima (suboptimal inventories).

3.1.1 Overview

The search algorithm used to find optimal consonant configurations is a form of hill-climbing, which takes as input five parameters:

- *numSegments*, the size of the consonant inventory that will be explored;
- *numRounds*, the number of iterations of the search algorithm;
- *numMutations*, the number of ‘mutations’ (neighbouring states) that is created for each segment per round;

¹<http://home.student.uva.nl/jan-willem.vanleussen>

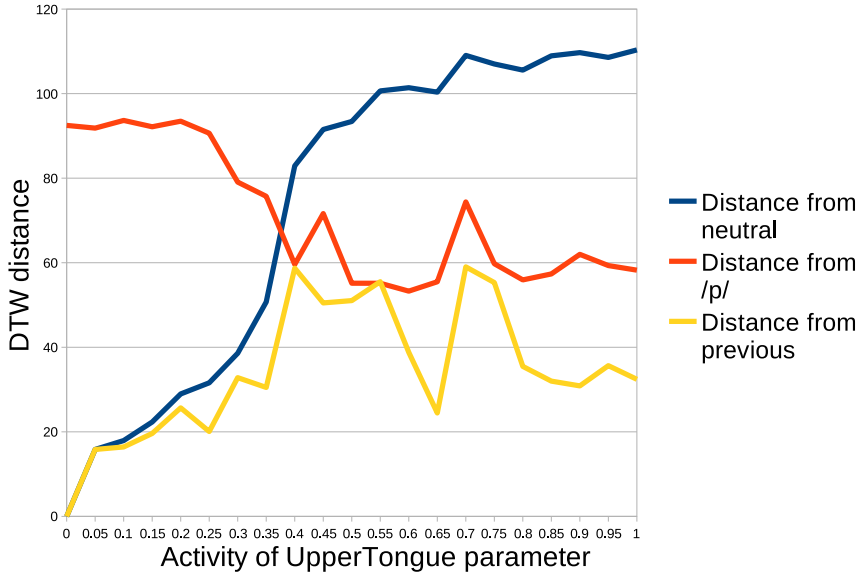


Figure 3.1: This graph shows the effect of varying the value of the *UpperTongue* parameter in an otherwise neutral articulation. It illustrates that the effect of increasing articulatory effort on perceptual distance is hard to predict. A comparison to a whole set of segments would likely show an even more complicated relationship.

- *maxTargets*, the maximum number of muscle parameters that may be active in a consonant segment;
- *effortWeight*, the relative importance of the effort parameter in the cost function.

A state in the search space is represented as a set of segments $\{s_1 \dots s_n\}$, where n represents the number of phoneme segments in the simulation *numSegments*. For *numRounds* iterations, the algorithm generates neighbouring states by creating *numMutations* of mutations s_x' of each segment. If the segment with the lowest cost among these mutations has a lower cost than the original segment, the new state $\{s_1 \dots s_x' \dots s_n\}$ will replace the old state.

In all simulations described in this paper, *numRounds* was set to 20, *numMutations* to 10 and *maxTargets* to 5. The values for *effortWeight* and *numSegments* were varied per simulation to test the effects of these parameters on the resulting inventories (Chapter 5.2). The following sections explain how the simulation is initialized and details the mutation process on segments.

3.1.2 Initialization

Each segment s in the total set of segments \mathcal{S} is initialized by selecting *maxTargets* muscle parameters at random from \mathcal{M} , and setting them to a random value between 0 and 0.3. This ensures that the initial set of segments are all slightly different while staying close to the neutral articulation. Next, all segments are synthesized in Praat and a (symmetric) matrix representing the mutual DTW distance between all pairs is calculated on the synthesized signals. The lowest nonzero number in each row of this matrix represents the *minimal mutual distance* between pairs containing that segment. Figure 3.2 shows an example of an initial segment set of 8 phonemes.

	s_1	s_2	s_3	s_4	s_5	s_6	s_7	s_8
s_1	0	62.31	55.17	37.36	60.11	51.05	38.90	47.63
s_2	·	0	33.70	50.44	25.56	35.62	58.32	40.59
s_3	·	·	0	45.82	30.34	27.78	52.63	34.66
s_4	·	·	·	0	48.98	37.39	35.01	37.30
s_5	·	(25.56)	·	·	0	33.92	56.69	38.60
s_6	·	·	·	·	·	0	44.74	20.18
s_7	·	·	·	(35.01)	·	·	0	41.55
s_8	·	·	·	·	·	(20.18)	·	0

Figure 3.2: An example DTW distance matrix. The lowest number in each row, representing the smallest distance between two segments in that row, is set in bold.

3.1.3 Mutations

After the set of segments \mathcal{S} has been initialized, the algorithm will proceed to cycle through the segments and create *numMutation* mutations of this segment. These mutations come in two types: *large* and *small*. A *large* mutation consists of picking a random muscle parameter from \mathcal{M} and assigning it a random value between 0 and 1. If there are already *maxTargets* active muscle parameters in the segment, a random active muscle will first be set to 0 (i.e. deactivated). Thus large mutations can result in very different articulations compared to the original segment.

A *small* mutation, on the other hand, does not add any new muscles to the list of active muscles, but rather changes the activity of an already active muscle by adding a small value to its activity a_m . This value is drawn from a normal distribution with a mean of zero and a standard deviation of 0.2. If the resulting activity value exceeds the upper limit of 1, it is clamped to 1. Likewise, if the resulting value is lower than zero, it will be set to zero, effectively removing this muscle parameter from the list of active targets. The changes wrought by a small mutation will usually have less impact on the resulting articulation.

A variable T determines the probability of choosing a small mutation rather than a large one; for each mutation, a random uniform number between 0 and 1 is generated. If this number is greater than T , a large mutation is made on the segment s ; else, a small mutation is made. The value of T increases linearly throughout the simulation, as its value is equal to the number of the current round divided by the total number of simulation rounds. In this way, the distance between the current state and neighbouring states becomes progressively smaller throughout the simulation.

Each of the mutated segments is synthesized in Praat, and DTW distances between it and the other segments in \mathcal{S} is calculated, so that the cost $f(s_{i_j})$ can be determined for each of the mutations $\{s_{i_1} \dots s_{inumMutations}\}$. The cost of the ‘best’ mutation s'_i is then compared to that of the original segment s_i ; if it is lower, the original segment is replaced by this mutation and the DTW matrix is updated to reflect the new distances.

3.2 Summary

A pseudocode overview of the main loop (Algorithm 1), the optimization procedure (Algorithm 2) and the mutation procedure (Algorithm 3) can be found in this section.

Algorithm 1 Initialization. (For this and subsequent algorithms, text in SMALL CAPS refers to another procedure; if this text is also UNDERLINED, it refers to an operation in Praat (Boersma and Weenink 2009)).

```

procedure MAIN(numRounds,numSegments,numMutations,maxTargets,effortWeight)
   $\mathcal{S} \leftarrow \emptyset$ 
  for  $i$  to numSegments do
    for  $j$  from 1 to maxTargets do                                      $\triangleright$  Initialize segments
      pick a random muscle ( $m_x | m_x \in \mathcal{M}$ )
       $a_{m_x} \leftarrow (\text{random}([0, 0.3])$ 
    end for
    SYNTHESIZE( $s_i$ )
    add  $s_i$  to  $\mathcal{S}$ 
  end for
  CALCULATE DTW DISTANCE MATRIX
   $\mathcal{S} \leftarrow \text{OPTIMIZE}(\mathcal{S}, \text{numRounds}, \text{numMutations}, \text{effortWeight})$ 
end procedure

```

Algorithm 2 Optimization. This is the main loop of the algorithm.

```

procedure OPTIMIZE( $\mathcal{S}$ , numRounds, numMutations, effortWeight)
   $w_e := \text{effortWeight}$ 
   $w_p := 1 - \text{effortWeight}$ 
  for  $\text{round}$  from 1 to numRounds do
     $T \leftarrow (\text{round} / \text{numRounds})$ 
    for  $s_i \in \mathcal{S}$  do
       $\text{Mutations}_i \leftarrow \emptyset$ 
      for  $j$  from 1 to numMutations do
         $s_{i_j} \leftarrow \text{MUTATE}(s_i, T)$ 
        add  $s_{i_j}$  to  $\text{Mutations}_i$ 
        SYNTHESIZE( $s_{i_j}$ )
         $f(s_{i_j}) = (w_d \cdot d(s_{i_j}) + w_e \cdot e(s_{i_j}))$ 
      end for
       $s'_i \leftarrow \text{arg min}(f(s_{i_j}) | s_{i_j} \in \text{Mutations}_i)$ 
      if  $f(s'_i) < f(s_i)$  then
         $s_i \leftarrow s'_i$ 
        UPDATE DTW MATRIX
      end if
    end for
  end for
  return  $\mathcal{S}$ 
end procedure

```

Algorithm 3 Mutation

procedure MUTATE(s, T) $activeMuscles = \text{all } m \in \mathcal{M} \text{ such that } a_m > 0 \text{ in } s\}$ **if** $T < \text{random}()$ **then**

▷ "Large" mutation

if $|activeMuscles| \geq \text{maxTargets}$ **then**pick a random muscle ($m_x | m_x \in activeMuscles$)set a_{m_x} to 0**end if**pick a random muscle ($m_x | m_x \in \mathcal{M}$)set a_{m_x} to a random value $[0,1]$ **else**

▷ "Small" mutation

pick a random muscle ($m_x | m \in activeMuscles$) $a'_{m_x} \leftarrow a_{m_x} + (\text{randomGauss}(\mu = 0, \sigma = 0.2))$ **if** $a'_{m_x} < 0$ **then**▷ Make sure $0 \leq a'_m \leq 1$ $a'_{m_x} \leftarrow 0$ **else if** $a'_{m_x} > 1$ **then** $a'_{m_x} \leftarrow 1$ **end if** $a_{m_x} \leftarrow a'_{m_x}$ **end if****return** s **end procedure**

Chapter 4

Evaluation method

In this chapter I will explain how my model of consonant optimization will be tested by comparing the simulation outcomes to actual spoken language data. In section 4.4, a number of hypotheses will be stated to test how well the model predicts trends and patterns found in natural consonant inventories.

4.1 Natural language data

The fact that we can speak with some certainty of phonological patterns in the languages of the world is mainly due to the efforts of numerous descriptive linguists, who have dedicated years to the study of previously undescribed languages in remote parts of the world. Data gathered in this manner have been compiled into various databases, such as the aforementioned UPSID¹ (Maddieson and Disner 1984) and P-BASE² (Mielke 2008). These databases aim to provide a representative sample of phonological inventories and processes in the languages of the world. Note that *representative* must not be interpreted in terms of number of speakers; the fact that roughly a third of the world's population speaks some form of Chinese, Spanish, English or Arabic (Lewis 2009) must be attributed to historical and political factors, not to properties of these languages. Instead, these databases are compiled such that as many language *families* (groupings of languages known to be related by common descent) as possible are represented.

Information in these phonological databases usually does not come in the form of audio recordings, but as classifications based on phonetic/phonological features (IPA symbols for P-BASE, an idiosyncratic encoding scheme for UPSID). This means that the notions of perceptual distinctiveness and articulatory effort (Chapter 2) cannot be applied directly to these data. To compare the outcome of the simulations to the crosslinguistic tendencies that can be found in these datasets, it is therefore necessary to first convert them to the same format, i.e. give some sort of phonological label to the results. The metric of DTW distance, discussed in Chapter 2.2.2, will also be used for converting the articulatory/acoustic data of the simulations to abstract phonological categories.

4.2 From auditory/articulatory data to phonemic classification

Although the articulatory synthesizer of Boersma was initially chosen for its ability to synthesize many different types of consonants found in language, the intrinsic and imposed limitations

¹<http://www.linguistics.ucla.edu/faciliti/sales/software.htm>

²<http://aix1.uottawa.ca/~jmielke/pbase/index.html>

Table 4.1: Overview of the 18 consonant labels assigned to the output of the model, sorted by *manner* (rows) and *place* (columns) of articulation. The place categories ‘labial’ and ‘labiodental’ have been merged; likewise, the coronal consonants and the palatal consonant /j/ have been grouped into a single place category. Gaps in the table represent sounds deemed articulatorily impossible, either in natural language or in the articulatory model.

	Labial	Coronal/palatal	Velar	Uvular	Pharyngeal
Plosive	p	t	k	q	
Trill		r		ʀ	
Fricative	β, v	ð	ɣ	ʁ	ʕ
(Lateral) approximant	w, ʋ	ɹ, l, j	ʍ		

described in section 2.1 diminish the amount of possible phoneme labelings that may result from the simulations:

- As the source of airflow in the model is determined through fixing the activity of the *Lungs* parameter during search, the results are limited to the class of pulmonic egressive sounds. This excludes **implosives** from appearing in the simulation.
- As the position of the larynx is fixed in search, **ejectives** will also not be generated in the simulations.
- Because timing differences between different articulatory gestures are not allowed under the constraints I put on Boersma’s model, **clicks** will not be present in the simulation results.
- The fixing of the tension of the vocal cords through the *Interarytenoid* parameter excludes **voicing distinctions**.
- The inability of Boersma’s model to accurately synthesize **nasals**, **sibilant fricatives** and **sibilant affricates** effectively excludes these classes from appearing in the simulation.

Based on these limitations, a set of 18 IPA symbols was chosen to label the segments; Table 4.1 displays an overview.

The most accurate method of labeling the sounds with these symbols would be to have a phonetically trained linguist annotate them manually. However, annotating the thousands of segments generated in the simulations by hand is a very labour-intensive task, and possibly introduces the danger of shaping the results toward a desired outcome. I therefore decided to automate the labeling of segments generated by the model, using the method of dynamic time warping on MFCCs described in section 2.2.2. For this I obtained four sets of comparison template consonants. Each of these sets contains recordings of a male phonetician pronouncing various consonant segments in an /a.a/ context.³ Figure 4.1 illustrates how the templates related to one another in perceptual space according to the DTW distance metric.

4.2.1 Incorporating articulatory features

As it turned out that labeling the sounds purely on the basis of auditory properties was quite inaccurate, I have decided to also use articulatory information in classifying the sounds. By

³These sets of recordings were created by Peter Ladefoged, Peter Isotalo, Paul Boersma and Jeff Mielke. The first two datasets are available online at <http://www.ladefogeds.com/vowels/contents.html> and http://commons.wikimedia.org/wiki/Category:General_phonetics respectively. The latter two were obtained from their respective authors.

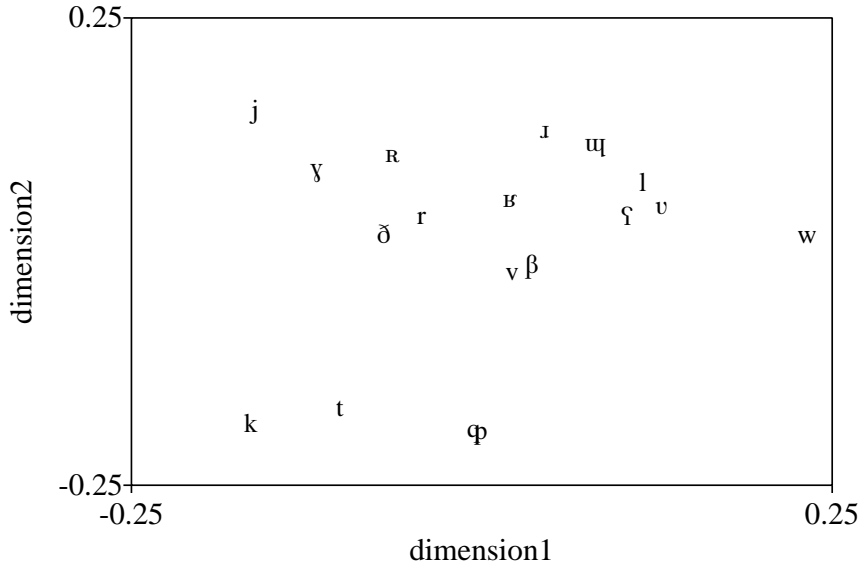


Figure 4.1: A scatterplot representing the DTW distances between the 18 template segments (averaged over four speakers) used to label the sounds resulting from the simulations. As in Figure 2.7 the 17-dimensional space has been reduced to two dimensions using individual difference scaling.

comparing the shape of the vocal tract in each segment to the shape of a neutral vocal tract, the tube in which the constriction is the smallest may be located. This tube is used to determine the *place* of articulation for the sound to be labeled, and limits the set of 18 labels from Table 4.1 to the subset with this place feature. If the vocal tract is not notably constricted at any point, the subset will be limited by manner of articulation APPROXIMANT instead. Next, dynamic time warping is performed on MFCC representations of the sound and the subset of template sounds to determine *manner* of articulation. Algorithm 4 details this procedure.

4.3 Phoneme frequency as a naturalness metric

Now that we have established a method to phonemically label the articulations emerging from the simulations, the results can be compared to the crosslinguistic databases mentioned in 4.1. The preferred approach would be to measure closeness of fit of the *inventories* to those found in natural languages, as for example de Boer (2001) and ten Bosch (1991) did for vowel systems. Unfortunately this is not feasible as the phonemic gaps listed in 4.2 are too large to meaningfully compare natural consonant systems to the simulation results. Nasal consonants, fricatives and voicing distinctions are quite common in natural systems, being present in approximately 98%, 91% and 68% of languages respectively (Maddieson 2008a), yet cannot be (completely) produced in the current version of the model. The size and variation of natural consonant inventories is therefore not reproducible in the model, making direct comparisons between inventories difficult.

An alternative approach, which is less affected by the phonemic gaps in the current model, is to measure optimality of inventories through the phonemic quality of individual phonemes. As Figure 1.1 shows, the distribution of different phonemes across languages is quite skewed; most phonemes occur only in a fraction of languages, while a handful of phonemes are present in the inventories of a large majority of languages. This supports the idea that certain individual phonemes are somehow intrinsically preferable to others, perhaps because they occupy a spot

Algorithm 4 Algorithm for labeling sounds

```
procedure LABELSOUND(s)
  CALCULATE VocalTracts from s
  for i to 175 do                                     ▷ (175 = number of tubes in neutral vocal tract)
    widthsi = width of tubei in VocalTracts
    widthneuti = width of tubei in VocalTractneut
    differencei =  $\frac{\text{width}_{s_i}}{\text{width}_{\text{neut}_i}}$ 
  end for
  smallestConstrictionIndex = argmini ∈ {1...175} (differencei)
  Calculate standard deviation of difference
  if standard deviation < 0.2 then
    Subset ← APPROXIMANT                               ▷ No notable constriction
    Subset ← APPROXIMANT                               ▷ Restrict to {/w/,/v/,/ɹ/,/j/,/l/,/ɹ̥/}
  else
    if smallestConstrictionIndex ≤ 65 then
      Subset ← PHARYNGEAL                               ▷ Restrict to {/ɹ̥/}
    else if smallestConstrictionIndex ≤ 70 then
      Subset ← UVULAR                                  ▷ Restrict to {/q/,/R/,/ɸ/}
    else if smallestConstrictionIndex ≤ 80 then
      Subset ← VELAR                                   ▷ Restrict to {/k/,/ɣ/,/ɰ/}
    else if smallestConstrictionIndex ≤ 160 then
      Subset ← CORONAL                                 ▷ Restrict to {/t/,/r/,/ð/,/j/,/l/,/ɹ̥/}
    else
      Subset ← LABIAL                                  ▷ Restrict to {/v/,/v̥/,/p/,/β/,/w/}
    end if
  end if
  SYNTHESIZE(s)
  for all 4 speakers in template sets do
    for all labels l in Subset do
      CALCULATE DTW DISTANCE(s, l)
    end for
    Normalize distances
  end for
  Calculate mean distance between speakers per label
  return label with lowest distance
end procedure
```

Table 4.2: Phoneme labels with their frequencies in P-BASE, and the \log_{10} of this percentage which is used as an index for phoneme optimality.

Label	Phoneme group	Frequency % in P-BASE	Log frequency score
/p/	/p/,/b/	97.81	1.99
/k/	/k/,/g/	93.24	1.97
/j/	/j/	88.50	1.95
/t/	/t/,/d/	83.75	1.92
/w/	/w/	78.83	1.90
/l/	/l/	78.46	1.90
/r/	/r/	59.67	1.78
/v/	/v/,/f/	58.39	1.77
/ʃ/	/ʃ/,/x/	29.19	1.47
/β/	/β/,/ϕ/	10.76	1.03
/q/	/q/,/ɣ/	10.03	1.00
/ɣ/	/ɣ/	7.48	0.87
/ð/	/ð/,/θ/	7.29	0.86
/v/	/v/	5.10	0.71
/ʕ/	/ʕ/,/ħ/	5.10	0.71
/ɪ/	/ɪ/	3.10	0.49
/ʉ/	/ʉ/	1.27	0.10
/ʀ/	/ʀ/	1.27	0.10

in the abstract auditory space of Figure 1.4 that is optimal in both auditory terms (distinctive from other possible consonants) and in articulatory terms (easy to produce). A good model of consonant inventories should therefore predict a larger frequency for these phonemes. For this reason, I use the estimated *frequency* of a given phoneme in natural language as a measure of optimality. The source for these frequency estimates is P-BASE (Mielke 2008), as it is the most recent and to my knowledge also largest (in terms of number of represented languages) phoneme database available.

For each of the phoneme labels in table 4.1, I have looked up the relative frequency percentage of this phoneme over all languages in P-BASE, i.e. the number of languages possessing this phoneme divided by the total number of languages in the database. In the case of articulations which allow voicing distinction in the basic IPA set (i.e. plosives and fricatives), the frequency of languages containing *any* phoneme of the voiceless/voiced pair was counted. The base 10 logarithm of these percentages was then used as the *frequency score* for a phoneme (see Table 4.3). The *naturalness* of an inventory is defined as the summed frequency score of all unique phonemes in the inventory, divided by the size of the simulated inventory *numSegments*. Inventories which contain a relatively large number or uncommon or *marked* phonemes will be scored as less ‘natural’. The next section will discuss a number of phenomena related to marked phonemes that should be explained by a model of consonant inventories, and which can be measured using the naturalness metric defined in this section.

4.4 Hypotheses

4.4.1 The size principle

A number of trends and common properties found in phoneme systems were briefly mentioned in Chapter 1. One such trend is that the size of a phoneme inventory correlates with the number of rare or uncommon phonemes it contains. This is quite visible in vowel inventories, where 3-vowel systems are almost exclusively made up out of the configuration $\{/a/, /i/, /u/\}$, while larger systems often contain these ‘corner vowels’ plus additional, rarer vowels. Computer simulations such as Liljencrants and Lindblom (1972) and de Boer (2001) confirm that this trend is replicated in computer simulations operating under simple phonetic principles. Lindblom and Maddieson (1988) show that the size principle also applies to consonant systems; smaller consonant inventories usually contain only members from a ‘basic set’ of about 20 consonants. Larger consonant inventories mostly consist of members from this set, plus other consonants which are more complex or ‘marked’.

Inventory size can be set as a parameter in the optimization model for consonant inventories described in this paper. In a correct model of consonant phoneme distributions, the number of rare segments in an inventory should correlate positively with the size of the simulated inventory. The ability of the model to account for the size principle can therefore be tested, using the *naturalness* metric defined in the previous section and the *numSegments* parameter defining the size of the segment inventory \mathcal{S} . This will be done in the next chapter.

4.4.2 Balancing maximal distinctiveness and minimal effort

In Chapter 1, the observation that phonemic systems balance between *maximal distinctivity* and *minimal articulatory effort* was made. For vowel systems, the first property was shown to be a deciding factor in the optimization model of Liljencrants and Lindblom (1972). The two properties were combined in the vowel optimization model of ten Bosch (1991), showing that conservation of effort may also play an important role in vowel systems.

Chapter 2 discussed how the two principles are formalized in a cost function for my optimization model of consonant inventories. If the organization of consonant inventories is organized along these lines, it is to be expected that some weighted *combination* of the effort cost and distinctivity cost will perform better, i.e. result in an inventory containing more common consonants, than just optimizing for optimal distinctivity. This hypothesis can be tested by setting the relative weight of the effort cost function to various nonzero values and observing the effect on the resulting inventories using the naturalness metric. A comparison of results under varying settings of the *effortWeight* parameter will be made in the next chapter.

Chapter 5

Results

In this chapter the simulation results are analyzed. First, an impressionistic analysis of the resulting phonemes and inventories is given. Next, the results are *quantitatively* analysed through the method described in 4.2, and the hypotheses put forward in 4.4 will be evaluated.

5.1 Qualitative analysis of results

Praat is able to draw a schematic representation of the vocal tract at any point during articulation. By taking several slices per second of an articulation and aligning these with the synthesized sound resulting from the articulation, I was able to generate movie files from the articulations. I used these movie files to obtain a general ‘impressionistic-phonetic’ description of the articulatory and acoustic properties of the results.

The resulting inventories generally show perceptual dispersal: several distinct consonants emerge from the simulations, especially in inventories of sizes 3 and 5. An interesting result is that the results are almost always *articulatorily* distinct, even though this was not an optimization criterion in any of the simulations. Rather, the optimization of perceptual distance seems to cause, as a side effect, utilization of different muscle groups per segment. Also of interest is that generally, *manner of articulation* seems to be the optimal way of making perceptual distinctions within the inventories: the 3-segment inventories often contain a plosive-like sound (usually /t/), a fricative-like sound (often /ʃ/) and an approximant-like sound. Figure 5.1 shows an example of a 5 segment-inventory found in the model.

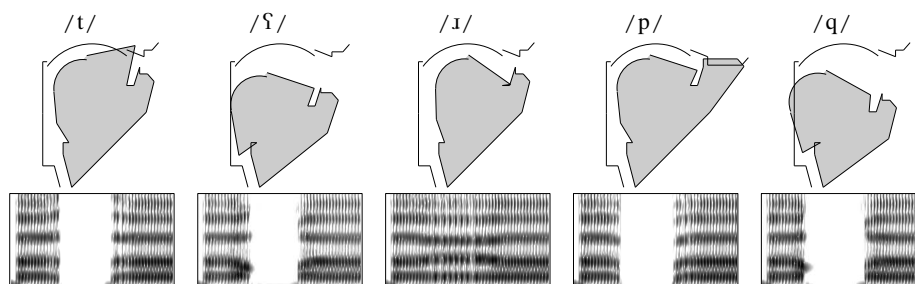


Figure 5.1: Schematic drawing (top) and spectrogram representation (bottom) of a 5-segment inventory that resulted from search (with *EffortWeight=0*). The phoneme symbols above the images are those assigned by the labeling algorithm.

When comparing the types of sounds resulting from the simulation runs to the phonemes of natural languages, the most glaringly wrong prediction of the model is that sounds which involve

a constriction very far back in the throat are quite abundant in the results. Natural languages containing these segments, however, are quite rare (Maddieson 2008b, Mielke 2008). Figure 5.2 shows a particular type of articulation that showed up quite often in the results, which was usually labeled as a pharyngeal fricative /ʕ/. The principally active muscle parameter in this type of articulation is *Mylohyoid*, which causes the jaw to move downwards and backwards; as it approaches 1, a constriction is created at the pharynx. If we assume that the rarity of these types of sounds are mainly due to conservation of effort, the conclusion must be that the effort function in the current version of the model is not yet sufficient.

Another shortcoming clearly visible in the results is that some of the resulting segments are nearly vocalic - that is, the constriction and resulting sound are nearer to a vowel than to a consonant. This is especially apparent in larger inventories and in simulations where the *effortWeight* parameter was set to a high value. The results were nevertheless labeled as approximant consonants, rather than vowels.

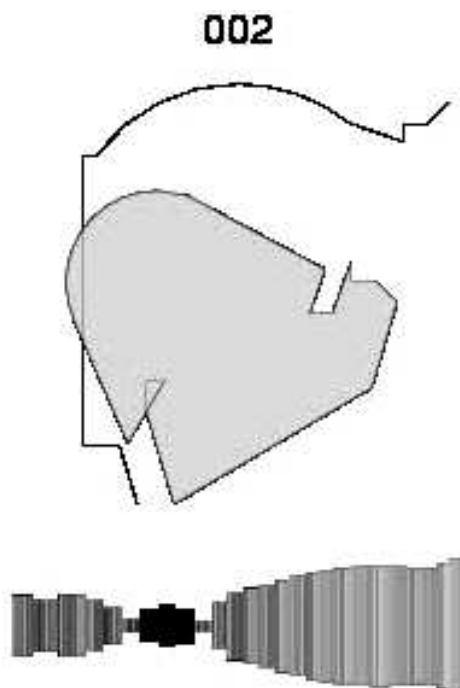


Figure 5.2: A still of the synthesized vocal tract during a segment that sounds like a pharyngeal fricative /ʕ/. This type of segment emerged often during the simulations, despite its rarity in natural language. The top of the picture shows a sagittal cross-section of the mouth and throat, the bottom represents the relative tube widths at different points in the vocal tract.

Chapter 6.2 discusses how the model might be improved to alleviate the general shortcomings listed above. The next section will provide a numerical analysis of the optimization results based on the phoneme labels assigned to the segments.

5.2 Quantitative analysis of results

In the course of a simulation run, the optimization algorithm tries to maximally disperse the segments in available acoustic space while minimizing the values of the different muscle parameters. Figure 5.3 shows the effect of this optimization on the DTW distance metric over the course of a single simulation run. The results generally show this type of pattern, with the

perceptual distance between phonemes quickly rising in the first few rounds of the simulation, after which growth tapers off steadily.

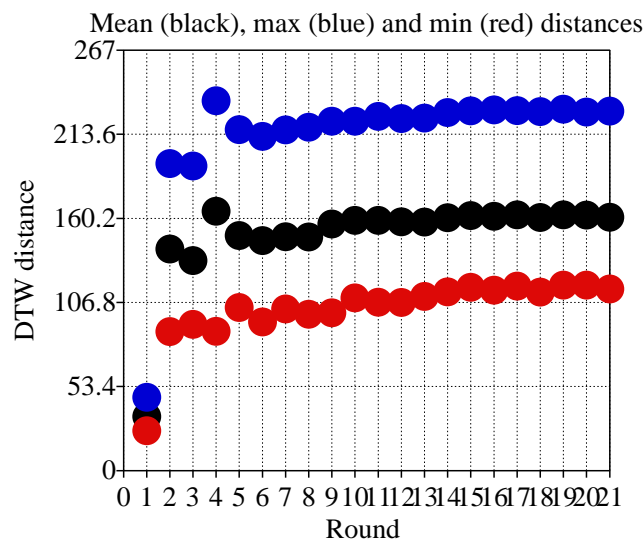


Figure 5.3: Minimum, mean and maximum DTW distance between segments in one run of the simulation (8 segments, relative effort weight at zero). The pattern shown here is typical for most of the simulation runs.

However, as [de Boer \(2006\)](#) points out, it is not particularly interesting or informative to show that an optimization algorithm which aims to minimize a cost function reaches a certain minimum. What we are interested in are the linguistic consequences of the optimization process: namely, if dispersion of consonants does indeed take place during the optimization procedure; and if so, under what parameters the end results resemble natural language most closely. For this, I will use the naturalness score of phonemes established in [4.3](#).

5.2.1 Overview

Table [5.2.1](#) gives an overview of the number of simulations executed to test the model under different values of the *effortWeight* and *numSegments* parameters. Effort weight was variously set to the values $\{0, 0.25, 0.5, 0.75, 0.9\}$. Since setting effort weight to 1 would trivially result in only ‘effortless’ neutral articulations, this was not attempted in the simulations. For each of these settings, inventories of sizes 3, 5 and 8 were created. At least 10 runs of the model were executed under each possible combination of these parameter settings; an additional 10 each were executed for *effortWeight*= 0, to get a more accurate view of the effect of inventory size independent of effort weight.

5.2.2 Results for individual phonemes

Figure [5.4](#) shows the distribution of segment labels after the final round at the end of all 180 simulations. When compared to the frequencies found for these phonemes in P-BASE (see Table [4.3](#)), it becomes clear that the predictions of the model are quite inaccurate in some respects. The phonemes /ʃ/, /v/ and /w/ are much more frequent in the simulation results than they are in natural language. The latter two, however, are especially frequent in the outcome of simulations where the *effortWeight* parameter has a relatively high value. Figure [5.4](#) also shows

Table 5.1: Overview of the number of simulation runs for the values of the *effortWeight* and *num-Phonemes* parameters

number of segments	3	5	8
<i>effortWeight</i> = 0	20	20	20
<i>effortWeight</i> = 0.25	10	10	10
<i>effortWeight</i> = 0.5	10	10	10
<i>effortWeight</i> = 0.75	10	10	10
<i>effortWeight</i> = 0.9	10	10	10

that these two approximant phonemes are much less likely to appear in the results if only perceptual distinctivity is taken into account.

The palatal approximant /j/ and the alveolar trill /r/ do not occur at all in the results, while both are attested in a majority of the languages represented in P-BASE. In the case of /r/, it might be that the specific limitations I have imposed on the articulatory model prevent this phoneme from emerging in search; Boersma (1998) reports that the articulatory model is able to synthesize an utterance sounding like /εεε/, but does not specify the settings of the articulatory parameters required to achieve this.

Two segments which are reported as very frequent in P-base, the bilabial plosive /p/ and the velar plosive /k/, are a lot rarer in the results. For instance the uvular plosive /q/ is more frequent in the resulting segments than the velar plosive /k/. In natural language, however, the reverse is the case: /k/ is nearly ubiquitous in the world’s languages, whereas /q/ is present in only about 10 percent of P-BASE languages. As with the overrepresentation of /ʕ/, it is likely the case that the amount of effort involved in making a uvular plosive is not reflected accurately in the effort metric.

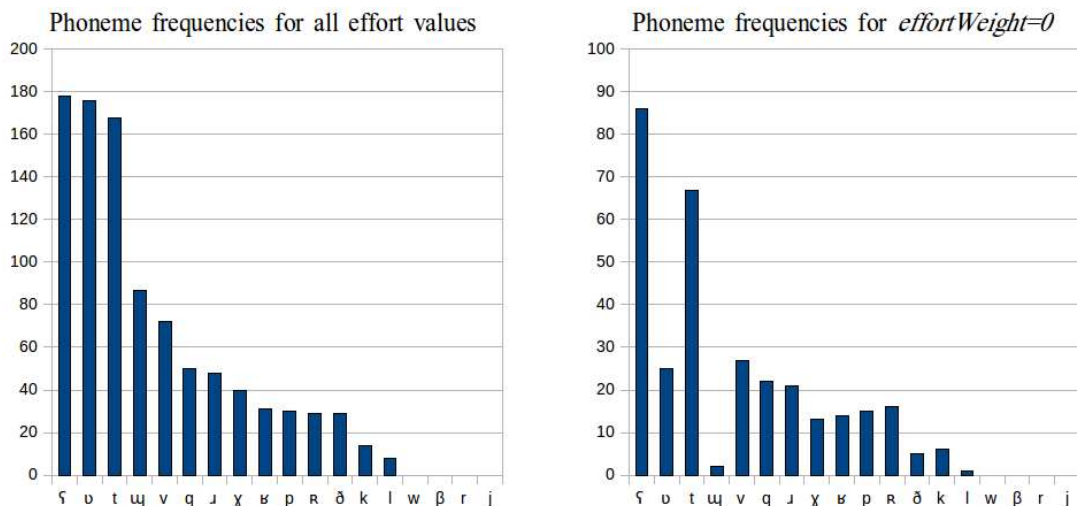


Figure 5.4: An overview of the frequencies of each of the phoneme labels in the end results for all simulations (left) and for simulations with *effortWeight=0* (right). Some rare phonemes like /ʕ/, /v/ and /ʉ/ occur quite often in the results; some phoneme labels are much less frequent when the relative weight of effort cost is low.

Table 5.2: p values of 2-sided t-tests comparing the effect of zero effort to the effort values 0.25, 0.5, 0.75 and 0.9. Degrees of freedom was 28 for all tests. Starred values are significant at $\alpha < 0.05$

	$w_e=0.25$	$w_e=0.5$	$w_e=0.75$	$w_e=0.9$
3 phonemes	0.39392	0.83581	0.49550	0.00002*
5 phonemes	0.56597	0.15946	0.17014	0.00001*
8 phonemes	0.94417	0.50545	0.15307	0.00000*

5.2.3 Effect of effort cost weight on naturalness

To test the effects of varying the effort parameter, the results for several simulation runs under differing values of the *effortWeight* parameter were compared to simulation runs with this parameter set to zero. Significance was tested using Student’s t-test (two-sided, $\alpha = 0.05$). Figure 5.5 and Table 5.2 summarize the results.

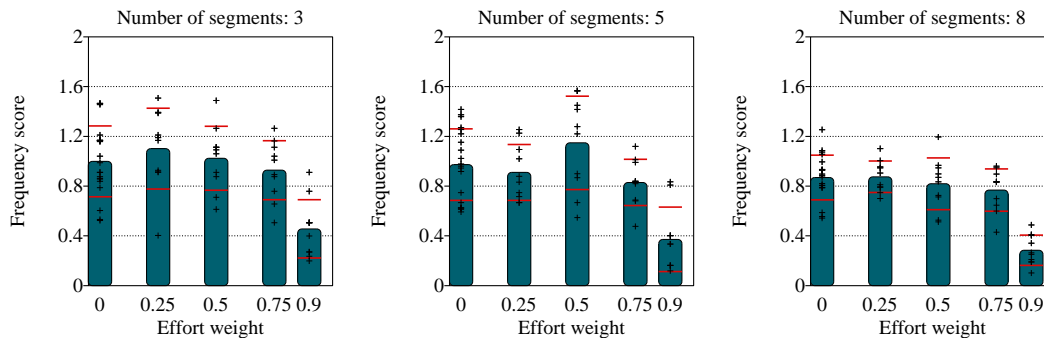


Figure 5.5: Comparing the effect of different values for the *effortWeight* parameter. The vertical axis shows the naturalness score (summed frequency score of all unique phoneme labels divided by *numSegments*). Red bars show plus and minus one standard deviation. Regardless of the number of segments, in the range from 0.25 to 0.75 no significant effect of effort is found; if effortWeight is 0.9, there is a significant negative effect on the naturalness of the resulting inventory.

The results show that for intermediate values (0.25, 0.5, 0.75) of the *effortWeight* parameter, no significant effect on the naturalness of the resulting inventories is found. If *effortWeight* is set to the high value of 0.9, there is a significant negative impact on naturalness of the results. This is caused by the large number of (relatively rare) approximant phonemes appearing in inventories generated under a high value for the effort weight parameter, as shown in the previous section.

5.2.4 Effect of inventory size on naturalness

Figure 5.6 shows the naturalness scores for inventories of 3, 5 and 8 segments under various values of the *effortWeight* parameter. To test the hypothesis that rarer phonemes should appear more often in larger inventories (as is generally the case in natural language), I calculated the Pearson’s ρ correlation coefficient between the value of the parameter *numSegments* and the naturalness score of the inventories generated with *effortWeight* = 0. The correlation is -0.214, which is not significant ($\alpha = 0.025$, one-tailed, $df=58$). This indicates that the model does not accurately predict the *size principle* (Lindblom and Maddieson 1988) acting on the consonant inventories of natural languages.

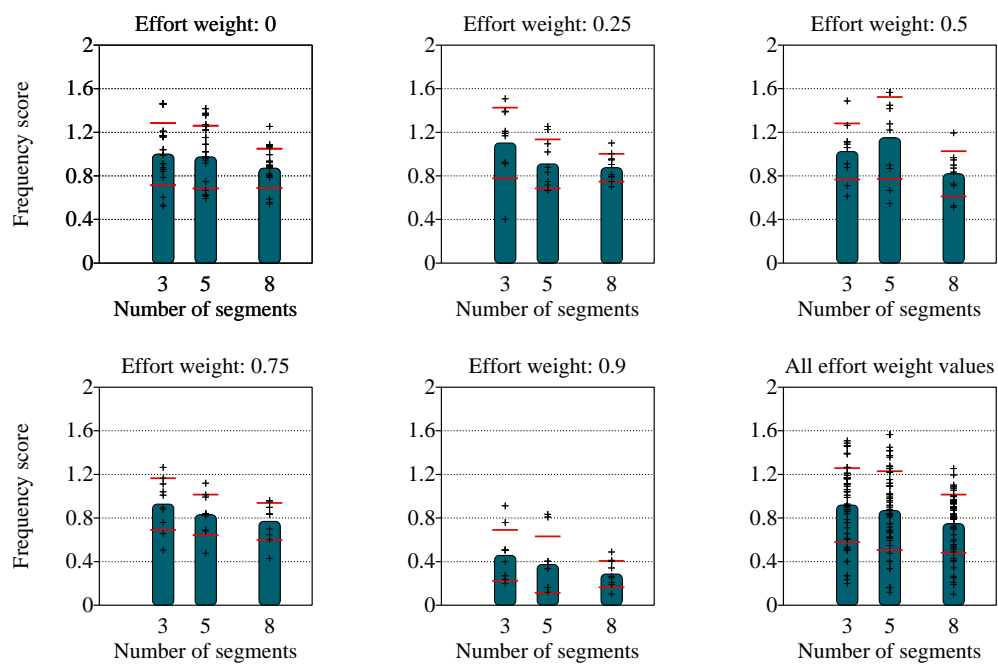


Figure 5.6: Effect of inventory size on naturalness. As in figure 5.5, the naturalness scores indicated on the vertical axis, and red bars indicate plus and minus one standard deviation.

Chapter 6

Conclusion and discussion

6.1 Summary and analysis of results

This paper presents a computational model of consonant inventories in natural language. The model is based on previous simulations of vowel systems, in which vowel configurations similar to those of natural languages were found by optimizing for maximal perceptual contrast and minimal articulatory effort. These results support an *emergentist* explanation of crosslinguistic patterns in phoneme inventories. Consonant inventories, although more diverse than vowel inventories, are often assumed to emerge under similar constraints. To extend the vowel optimization methods to the more complex domain of consonants, a novel optimization method was developed. This method uses an articulatory synthesizer (Boersma 1998) to explore the articulatory and acoustic space available in consonant production, and a model of acoustic dispersion based on Dynamic Time Warping (DTW) of pairs of signals thus synthesized. DTW was also used to give a phonemic label to the resulting sound signals.

The articulatory model used to produce consonants was regrettably found to be incapable of synthesizing a number of consonant sounds that are quite abundant in natural language. As a consequence, the phonemic repertoire available to the optimisation model is limited in comparison to that of real speakers. Because of this, direct comparison of the configurations emerging from the model to those found in the various languages and language families of the world was not feasible. Instead, an alternative evaluation method was developed, in which the *naturalness* of an inventory was defined as a function of the *relative frequencies* of its members in a database of phonological inventories (P-BASE, Mielke 2008).

A qualitative analysis of the resulting inventories confirmed that dispersion of consonants takes place in the optimization algorithm. As in natural language, certain phonemes were present in the inventories much more frequently than others; at the same time no single ‘optimal’ solution emerged from the results. This is probably due to the complex shape of the optimization landscape, and in fact reflects the diversity of consonant systems found in language (there is generally much greater variety for consonants than there is for vowels). However, the results are not very accurate with respect to the quality of the resulting consonants. Consonant phonemes which are abundant in natural languages, such as /k/, /j/ and /p/, were absent or only marginally present in the simulation results. At the same time, several phonemes which occur only rarely in natural language such as /ʕ/ and /q/ are quite frequent in the labeled results. Generally, the model seems too inclined towards consonants made in the back of the oropharyngeal cavity. The optimality of these consonants according to the model is not reflected in natural language data.

The naturalness metric was used to test two hypotheses. The first concerns the *size principle*, which states that there is a positive correlation between the number of phonemes in an inventory

and the relative number of rare or more complex phonemes it contains. This would translate to a lower naturalness for larger inventories in the model. However, no significant correlation was found between the number of phonemes modeled and the naturalness scores of the resulting inventories. The second hypothesis concerned the proposed balance between maximal inter-phoneme distinctiveness and minimal articulatory effort. Simulation results did not confirm that these constraints apply to consonant inventories: varying the relative weight of articulatory effort in the cost function did not have a significant positive effect on naturalness.

Quantitative analysis of the results thus supports the conclusion that unlike vowel inventories, patterns in consonant inventories do not emerge from a combination of the phonetic principles of minimal effort and maximal distinctiveness. However, I believe the qualitative analysis suggests that the optimization approach may not be a dead end. The overrepresentation of crosslinguistically rare segments in the results indicates that some aspects of consonant inventory optimality are not represented faithfully in the current version of the model. The next section therefore lists a number of improvements that could be made on the model to better account for linguistic data.

6.2 Future work

6.2.1 Improving the optimization model

As set out in chapter 2.1, the articulatory model of Boersma (1998) used in the optimization model described in this paper was constrained in a number of ways. Some of these constraints are intrinsic to the synthesizer, such as the inability to accurately synthesize sibilants and nasals. I imposed additional constraints to limit the size of the search space. Abstracting from certain properties of sounds is to some extent necessary in a phonetic model, but in this case the predictive power of the model is too severely hampered by the abstractions. Given its inability to synthesize the important classes of nasal and sibilant consonants, in retrospect the articulatory model of Boersma does not suffice for accurate modelling of consonant inventories. In order to improve the optimization model it will therefore be necessary to either switch to another articulatory model, such as that of Birkholz (2005), or to extend Boersma’s model so that it can account for a richer set of sounds. Increasing the phonetic space available to the model will also allow for a better comparison of model output to natural language data.

While increasing weight of the effort cost parameter was shown to impact the results, it did not have the hypothesized effect of increasing naturalness of the resulting inventories. I believe this does not disprove the notion of *conservation of effort*; rather, the effort cost function introduced in this paper likely does not reflect actual articulatory effort well enough. A first step towards improving the effort cost function is probably to increase the differences in effort cost for individual muscle parameters; particularly the articulations resulting in uvular and pharyngeal constrictions should be punished more severely in the effort cost function. The assumption that effort is directly determined by muscle activity may also be too naive. Considerations like the precision required for a gesture (or robustness to articulatory fluctuations, see Stevens 1972) may also contribute to the concept of articulatory effort.

Perceptual distance is defined purely in auditory terms in the current model. However, while not strictly necessary to acquire and use speech, visual perception also plays an important role in speech perception, aiding in discriminating speech distorted by noise (Sumbly and Pollack 1954) and able to overrule auditory information under certain circumstances (McGurk and MacDonald 1976). It is plausible that visually distinct articulations, like bilabials, may be generally preferred in the world’s languages for these reasons. The lack of a visual modality in the current model may be partially responsible for the unrealistic proclivity toward sounds made in the

back of the throat.

In terms of evaluation of the results, the automatic labeling of simulated phonemes through DTW comparison with template phonemes is another component of the model that can be improved. While manually labeling large numbers of synthesized phonemes is too labour-intensive to classify all results by hand, the classification algorithm could be improved through supervised training on a number of hand-labeled examples. For a more principled analysis of the results, it is also necessary to develop an evaluation method which is able to compare resulting inventories *as a whole* to the inventories of natural languages, instead of basing naturalness of inventories on properties of its individual members. A feature-based approach similar to that of Mielke (2005) might be taken here.

Finally, the current model could be improved by modelling sound variation in a larger context. As is, the model only allows for limited variation within a static /ə_ə/ context. This serves to keep the search space of the model, and the range of possible results, within reasonable limits. Actual articulation of speech sounds, however, is often conditioned by the phonemic environment in which the sound occurs. A more thorough model of consonant inventories should therefore be able to account for this, for instance by allowing more variation on the vowel context surrounding the synthesized consonants.

6.2.2 Towards a non-teleological, speaker-oriented model

The model described in this paper optimizes at the level of the *language*. While many common sound changes and inventory states can be stated in terms of global processes such as acoustic dispersion and effort minimization, this ultimately does not explain the mechanisms responsible for sound change and inventory formation. Rather, these global processes are thought to be set in motion by local processes at the level of the speaker and hearer (Ohala 1981, Blevins 2004). Computer simulations confirm that optimal phoneme inventories may emerge as a result of small-scale interactions between simulated individuals (*agents*) who do not explicitly aim to optimize the inventory (de Boer 2001).

Many of the components of the current model, such as the use of articulatory synthesis and the use of techniques from speech recognition to define perceptual similarity or distance, could probably be incorporated without much trouble in an agent-based model of consonant inventories. An agent-based model could also incorporate the concept of *learnability*, reflecting the fact that some articulations are more difficult to master than others, and that learned motor gestures can be reused in other articulations. However, as the computational cost of realistic articulatory synthesis is quite high at the moment of writing, the computing power required for modelling even a modest number of interacting agents equipped with such a synthesizer may yet be too substantial.

Chapter 7

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